## Programming Languages and Compilers (CS 421)

## William Mansky

## http://courses.engr.illinois.edu/cs421/su2013/

Based in part on slides by Mattox Beckman, as updated by Vikram Adve, Gul Agha, and Elsa Gunter

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## Course Website

- http://courses.engr.illinois.edu/cs421/su2013/
- Main page - summary of news items
- Policy - rules governing course
- Lectures - syllabus and slides
- MPs - information about homework
- Exams
- Unit Projects - for 4 credit students
- Resources - tools and helpful info
- FAQ


## Piazza

- Class discussion board on http://piazza.com
- Post questions about course, assignments, exams, etc.
- Instructor and TA check once/day
- Collaboration on HWs/MPs is allowed, but you must write and test your code separately (see policy for details)


## Some Course References

- No required textbook.
- Essentials of Programming Languages (2nd Edition) by Daniel P. Friedman, Mitchell Wand and Christopher T. Haynes, MIT Press 2001.
- Compilers: Principles, Techniques, and Tools, (also known as "The Dragon Book"); by Aho, Sethi, and Ullman. Published by Addison-Wesley. ISBN: 0-201-10088-6.
- Modern Compiler Implementation in ML by Andrew W. Appel, Cambridge University Press 1998
- Additional ones for OCaml given separately


## Course Grading

- Homework 20\%
- About 9 MPs (in OCaml) and 8 written assignments
- MPs submitted by handin on EWS linux machines
- Late submission penalty: $20 \%$ of assignments total value
- 2 Midterms - 20\% each
- In class - June 27, July 18
- DO NOT MISS EXAM DATES!
- Final 40\% - Aug 4 1PM - 3PM
- Percentages are approximate
- Exams may weigh more if homework is much better


## Course Homework

- You may discuss homeworks and their solutions with others
- You may work in groups, but you must list members with whom you worked if you share solutions or solution outlines
- Each student must turn in their own solution separately
- You may look at examples from class and other similar examples from any source
- Note: University policy on plagiarism still holds - cite your sources if you are not the sole author of your solution
- Problems from homework may appear verbatim, or with some modification on exams


## Course Objectives

- New programming paradigm
- Functional programming
- Tail Recursion
- Continuation Passing Style
- Phases of an interpreter / compiler
- Lexing and parsing
- Type checking
- Evaluation
- Programming Language Semantics
- Lambda Calculus
- Operational Semantics


## OCaml

- Compiler is on the EWS-linux systems
- A (possibly better, non-PowerPoint) text version of this lecture can be found at
- http://courses.engr.illinois.edu/cs421/su201 3/lectures/ocaml-intro-shell.txt
- For the OCaml code for today' s lecture see
- http://www.cs.illinois.edu/class/cs421/lectur es/ocaml-intro.ml


## WWW Addresses for OCaml

- Main CAML home: http://caml.inria.fr/index.en.html
- To install OCaml on your computer see:
- http://caml.inria.fr/ocaml/release.en.html


## References for CAML

- Supplemental texts (not required):
- The Objective Caml system release 4.00, by Xavier Leroy et al., online manual
- Introduction to the Objective Caml Programming Language, by Jason Hickey
- Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O' Reilly - Available online from course resources


## OCaml

- CAML is European descendant of original ML - American/British version is SML
- O is for object-oriented extension
- ML stands for Meta-Language
- ML family designed for implementing theorem provers
- Despite obscure original application area, OCaml is a full general-purpose programming language


## Features of OCaml

- Higher order applicative language
- Static Types
- Call-by-value parameter passing
- Modern syntax
- Parametric polymorphism
- Aka structural polymorphism
- Automatic garbage collection
- User-defined algebraic data types


## Why learn OCaml?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCaml is particularly efficient for programming tasks involving languages (e.g. parsing, compilers, user interfaces)
- Used at Microsoft for writing SLAM, a formal methods tool for C programs


## Session in OCaml

\% ocaml
Objective Caml version 4.00
\# (* Read-eval-print loop; expressions and declarations
$2+3 ; ; \quad$ (* Expression *)

- : int = 5
\# 3 < 2;;
- : bool = false


## No Overloading for Basic Arithmetic Operations

\＃ 15 ＊2；；
－：int＝ 30
\＃ $1.35+0.23 ;$ ；（＊Wrong type of addition＊）
Characters 0－4：
$1.35+0.23 ;$ ；（＊Wrong type of addition＊）
ヘヘヘヘ
Error：This expression has type float but an expression was expected of type int
\＃ 1.35 ＋0．23；；
－：float＝ 1.58

## No Implicit Coercion

\# 1.0 * 2;; (* No Implicit Coercion *)
Characters 0-3:

$$
\left.\begin{array}{l}
1.0 * 2 ; ~(* \text { No Implicit Coercion *) } \\
\wedge \wedge \wedge
\end{array}\right)
$$

Error: This expression has type float but an expression was expected of type int

## Sequencing Expressions

\# "Hi there";, (* has type string *)

- : string = "Hi there"
\# print_string "Hello world\n";, (* has type unit *) Hello world
- : unit = ()
\# (print_string "Bye\n"; 25);; (* Sequence of exp *)
Bye
- : int = 25


## Terminology

- Output refers both to the result returned from a function application
- As in + outputs integers, whereas +. outputs floats
- And to text printed as a side-effect of a computation
- As in print_string " n " outputs a carriage return
- In terms of values, it outputs ( ) ("unit")
- We will standardly use "output" to refer to the value returned


## Declarations; Sequencing of Declarations

\# let $\mathrm{x}=2+3 ;$; (* declaration $*)$
val $x$ : int $=5$
\# let test = $3<2$;;
val test : bool = false
\# let $\mathrm{a}=3$ let $\mathrm{b}=\mathrm{a}+2$; ; (* Sequence of dec *)
val a : int = 3
val b:int=5

## Environments

- Environments record what value is associated with a given variable
- Central to the semantics and implementation of a language
- Notation

$$
\rho=\left\{\text { name }_{1} \rightarrow \text { value }_{1}, \text { name }_{2} \rightarrow \text { value }_{2}, \ldots\right\}
$$

Using set notation, but describes a partial function

- Often stored as list, or stack
- To find value start from left and take first match


## Global Variable Creation

\# 2 + 3;; (* Expression *)
// doesn' t effect the environment
\# let test = $3<2 ;$; (* Declaration *)
val test : bool = false
// $\rho=\{$ test $\rightarrow$ false $\}$
\# let $\mathrm{a}=3$ let $\mathrm{b}=\mathrm{a}+2$; ; (* Sequence of dec *)
$/ / \rho=\{b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$

## Local let binding

// $\rho=\{b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# let b=5*4in 2*b;,

- : int = 40
// $\rho=\{b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# let c =
let $\mathrm{b}=\mathrm{a}+\mathrm{a}$
in $b$ * $b ;$;
val c : int = 36
// $\rho=\{c \rightarrow 36, b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# b;;
- : int = 5

5/28/2013

## Local Variable Creation

\# let c =
let $b=a+a$
$/ / \rho_{1}=\{b \rightarrow 6, a \rightarrow 3$, test $\rightarrow$ false $\}$
in $b$ * $b_{;} ;$
val c: int $=36$
$/ / \rho=\{c \rightarrow 36, b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# b;;

- : int = 5


## Booleans (aka Truth Values)

\# true;;

- : bool = true
\# false;;
- : bool = false

$$
\begin{aligned}
& \text { \# if } y>x \text { then } 25 \text { else 0;; } \\
& -: \text { int }=25
\end{aligned}
$$

## Booleans

\# 3 > 1 \&\& 4 > 6;;

- : bool = false
\# 3 > $1|\mid 4$ > 6;;
- : bool = true
\# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
Hi
- : bool = true
\# 3 > 1 || (print_string "Bye\n"; 4 > 6) ;;
- : bool = true
\# not (4 > 6);",
- : bool = true


## Tuples

\# let s = (5,"hi", 3.2);;
val s : int * string * float = (5, "hi", 3.2)
\# let $(\mathrm{a}, \mathrm{b}, \mathrm{c})=\mathrm{s} ; ; \quad\left(*(\mathrm{a}, \mathrm{b}, \mathrm{c})\right.$ is a pattern $\left.{ }^{*}\right)$
val a : int = 5
val b: string = "hi"
val c: float $=3.2$
\# let $x=2,9.3 ;$; (* tuples don't require parens in OCaml *)
val $x$ : int * float $=(2,9.3)$

## Tuples

\# (*Tuples can be nested *)
let d = ((1,4,62),("bye",15),73.95);,;
val d : (int * int * int) * (string * int) * float $=$
((1, 4, 62), ("bye", 15), 73.95)
\# (*Patterns can be nested ${ }^{*}$ )
let (p,(st,_),_) = d;; (* _ matches all, binds nothing *)
val $p$ : int * int * int $=(1,4,62)$
val st : string = "bye"

## Functions

\# let plus_two $\mathrm{n}=\mathrm{n}+2$; ; val plus_two : int -> int = <fun> \# plus_two 17;;

- : int = 19
\# let plus_two $=$ fun $\mathrm{n}->\mathrm{n}+2 ;$;
val plus_two : int -> int = <fun>
\# plus_two 14;;
- : int = 16

First definition syntactic sugar for second

## Using an anonymous function

\# (fun x->x * 3) 5;; (* An application *)
$-:$ int $=15$
\# ((fun y -> y +. 2.0), (fun z-> z * 3));; (* As data *)

- : (float -> float) $*$ (int -> int) $=(<$ fun $>$, <fun>)

Note: in fun $v->\exp (v)$, scope of variable is only the body $\exp (\mathrm{v})$

## Values fixed at declaration time

\# let $\mathrm{x}=12$;
val x : int = 12
\# let plus_x y = y + x; ;
val plus_x : int -> int = <fun>
\# plus_x 3;;

What is the result?

## Values fixed at declaration time

\# let $\mathrm{x}=12$;
val x : int $=12$
\# let plus_x y = y + x ;;
val plus_x : int -> int = <fun>
\# plus_x 3;;

- : int = 15


## Values fixed at declaration time

\# let $\mathrm{x}=7$; ; (* New declaration, not an update *)
val x : int = 7
\# plus_x 3;;

What is the result this time?

## Values fixed at declaration time

\# let x = 7;; (* New declaration, not an update *)
val x : int = 7
\# plus_x 3;;

- : int = 15


## Functions on tuples

\# let plus_pair (n,m) = n + m;;
val plus_pair : int * int -> int = <fun>
\# plus_pair $(3,4)$;,

- : int = 7
\# let double $x=(x, x)$; ;
val double : 'a -> 'a * 'a = <fun>
\# double 3;;
- : int * int $=(3,3)$
\# double "hi";;
- : string * string = ("hi", "hi")


## Match Expressions

\# let triple_to_pair triple =

$$
\begin{aligned}
& \text { match triple } \\
& \text { with }(0, x, y)->(x, y)
\end{aligned}
$$

-Each clause: pattern on left, expression on right

$$
\begin{aligned}
& \mid(x, 0, y)->(x, y) \\
& \mid(x, y,-)->(x, y) ; \prime
\end{aligned}
$$ -Each $x, y$ has scope of only its clause

- Use first matching clause
val triple_to_pair : int * int * int -> int * int = <fun>


## Functions with more than one argument

\# let add_three x y z = x + y + z;;;
val add_three : int -> int -> int -> int = <fun>
\# let t = add_three 63 2;;
val t : int = 11

## Curried vs Uncurried

- Recall
val add_three : int -> int -> int -> int = <fun>
- How does it differ from
\# let add_triple ( $\mathrm{u}, \mathrm{v}, \mathrm{w}$ ) = u + v + w; ;
val add_triple : int * int * int -> int = <fun>
- add_three is curried;
- add_triple is uncurried


## Partial application of functions

## let add_three x y $\mathrm{z}=\mathrm{x}+\mathrm{y}+\mathrm{z}$; ;

\# let h = add_three 5 4;;
val h : int -> int = <fun>
\# h 3;;

- : int = 12
\# h 7;;
- : int = 16


## Curried vs Uncurried

\＃add＿triple（6，3，2）；；
－：int＝ 11
\＃add＿triple 5 4；；
Characters 0－10：
add＿triple 5 4；； ヘヘヘヘヘヘヘヘヘヘヘ

This function is applied to too many arguments， maybe you forgot a｀；＇
\＃fun x－＞add＿triple（ $5,4, \mathrm{x}$ ）；，
：int－＞int＝＜fun＞

## Functions as arguments

\# let thrice $\mathrm{fx}=\mathrm{f}(\mathrm{f}(\mathrm{fx})$ ); ;
val thrice : ('a -> 'a) -> 'a -> 'a = <fun> \# let g = thrice plus_two;;
val g : int -> int = <fun>
\# g 4;;

- : int = 10
\# thrice (fun s -> "Hi! " ^ s) "Good-bye!";;
- : string = "Hi! Hi! Hi! Good-bye!"


## Question

- Observation: Functions are first-class values in this language
- Question: What value does the environment record for a function variable?
- Answer: a closure


## Save the Environment!

- A closure is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:

$$
\mathrm{f} \rightarrow\left\langle(\mathrm{v} 1, \ldots, \mathrm{vn}) \rightarrow \exp , \rho_{\mathrm{f}}\right\rangle
$$

- Where $\rho_{f}$ is the environment in effect when $f$ is defined (if $f$ is a simple function)


## Closure for plus_x

- When plus_x was defined, had environment:

$$
\rho_{\text {plus_ }}=\{x \rightarrow 12, \ldots, y \rightarrow 24, \ldots\}
$$

- Closure for plus_x:

$$
<y \rightarrow y+x, \rho_{\text {plus_x }}>
$$

- Environment just after plus_x defined:
$\left\{\right.$ plus_x $\rightarrow\left\langle y \rightarrow y+x, \rho_{\text {plus_ }}>\right\}+\rho_{\text {plus_x }}$


## Combining Environments

- We combine environments with +
- Almost like set union
- Conflicts are resolved in a left-biased manner

$$
.\{y \rightarrow 3, x \rightarrow 7\}+\{y \rightarrow 9, \ldots\}=\{y \rightarrow 3, x \rightarrow 7, \ldots\}
$$

## Evaluation of Application with Closures

- In environment $\rho$, evaluate left term to closure, $c=\left\langle\left(x_{1}, \ldots, x_{n}\right) \rightarrow b, \rho\right\rangle$
- ( $\mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}}$ ) variables in (first) argument

Evaluate the right term to values, $\left(\mathrm{v}_{1}, \ldots, \mathrm{v}_{\mathrm{n}}\right)$
Update the environment $\rho$ to
$\rho^{\prime}=\left\{\mathrm{X}_{1} \rightarrow \mathrm{v}_{1}, \ldots, \mathrm{X}_{\mathrm{n}} \rightarrow \mathrm{v}_{\mathrm{n}}\right\}+\rho$

- Evaluate body b in environment $\rho^{\prime}$


## Evaluation of Application of plus_X; ;

- Have environment:

$$
\begin{gathered}
\rho=\left\{\text { plus_ } x \rightarrow<y \rightarrow y+x, \rho_{\text {plus_x }}>, \ldots,\right. \\
y \rightarrow 3, x \rightarrow 7, \ldots\}
\end{gathered}
$$

where $\rho_{\text {plus_x }}=\{x \rightarrow 12, \ldots, y \rightarrow 24, \ldots\}$

- Eval (plus_x y, $\rho$ ) rewrites to
- Eval $\left(<y \rightarrow y+x, \rho_{\text {plus_x }}>3, \rho\right)$ rewrites to
- Eval $\left(y+x,\{y \rightarrow 3\}+\rho_{\text {plus_x }}\right)$ rewrites to
- Eval $\left(3+12, \rho_{\text {plus_x }}\right)=15$


## Scoping Question

Consider this code:
let $x=27 ;$;
let $\mathrm{f} x=$
let $x=5$ in
(fun x -> print_int x) 10; ;
f 12; ;
What value is printed?
5
10
12
27

## Scoping Question

Consider this code:
let $x=27 ;$;
let $\mathrm{f} x=$
let $x=5$ in
(fun x -> print_int x) 10; ;
f 12; ;
What value is printed?
5
10
12
27

