Programming Languages and Compilers (CS 421)

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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

Recursive Descent Parsing

- Recursive descent parsers are a class of parsers derived fairly directly from BNF grammars
- A recursive descent parser traces out a parse tree in top-down order, corresponding to a left-most derivation (LL - left-to-right scanning, leftmost derivation)

Recursive Descent Parsing

- Each nonterminal in the grammar has a subprogram associated with it; the subprogram parses all phrases that the nonterminal can generate
- Each nonterminal in right-hand side of a rule corresponds to a recursive call to the associated subprogram

Recursive Descent Parsing

- Each subprogram must be able to decide how to begin parsing by looking at the left-most character in the string to be parsed
  - May do so directly, or indirectly by calling another parsing subprogram
- Recursive descent parsers, like other top-down parsers, cannot be built from left-recursive grammars
  - Sometimes can modify grammar to suit

Sample Grammar

<expr> ::= <term> | <term> + <expr>
| <term> - <expr>

<term> ::= <factor> | <factor> * <term>
| <factor> / <term>

<factor> ::= <id> | (<expr>)

Tokens as OCaml Types

- + - * / ( ) <id>
- Becomes an OCaml datatype

```
type token =
    Id_token of string
  | Left_parenthesis | Right_parenthesis
  | Times_token | Divide_token
  | Plus_token | Minus_token
```

Parse Trees as Datatypes

<expr> ::= <term> | <term> + <expr>
| <term> - <expr>

```
type expr =
    Term_as_Expr of term
  | Plus_Expr of (term * expr)
  | Minus_Expr of (term * expr)
```


Parse Trees as Datatypes

<term> ::= <factor> | <factor> * <term>
| <factor> / <term>

```
and term =
    Factor_as_Term of factor
  | Mult_Term of (factor * term)
  | Div_Term of (factor * term)
```


Parse Trees as Datatypes

<factor> ::= <id> | (<expr>)

```
and factor =
    Id_as_Factor of string
  | Parenthesized_Expr_as_Factor of expr
```


Parsing Lists of Tokens

- Will create three mutually recursive functions:
  - expr : token list -> (expr * token list)
  - term : token list -> (term * token list)
  - factor : token list -> (factor * token list)
- Each parses what it can and gives back parse and remaining tokens

Parsing an Expression

<expr> ::= <term> [(+ | -) <expr>]

```
let rec expr tokens =
  (match term tokens
    with ( term_parse , tokens_after_term) ->
      (match tokens_after_term
        with( Plus_token  :: tokens_after_plus) ->
```


Parsing an Expression

<expr> ::= <term> [(+ | -) <expr>]

```
let rec expr tokens =
  (match term tokens
    with ( term_parse , tokens_after_term) ->
      (match tokens_after_term
        with ( Plus_token  :: tokens_after_plus) ->
```

Parsing a Plus Expression

<expr> ::= <term> [(+ | -) <expr>]

```
let rec expr tokens =
  (match term tokens
    with ( term_parse , tokens_after_term) ->
      (match tokens_after_term
       with ( Plus_token  :: tokens_after_plus) ->
```


Parsing a Plus Expression

<expr> ::= <term> [(+ | -) <expr>]

```
let rec expr tokens =
  (match term tokens
    with ( term_parse , tokens_after_term) ->
      (match tokens_after_term
       with ( Plus_token  :: tokens_after_plus) ->
```


Parsing a Plus Expression

<expr> ::= <term> [(+ | -) <expr>]

```
let rec expr tokens =
  (match term tokens
    with ( term_parse , tokens_after_term) ->
      (match tokens_after_term
       with ( Plus_token  :: tokens_after_plus) ->
```


Parsing a Plus Expression

<expr> ::= <term> + <expr>

```
(match expr tokens_after_plus
  with ( expr_parse  , tokens_after_expr) ->
  ( Plus_Expr  ( term_parse  ,  expr_parse ),
   tokens_after_expr))
```


Parsing a Plus Expression

<expr> ::= <term> + <expr>

```
(match expr tokens_after_plus
  with ( expr_parse  , tokens_after_expr) ->
  ( Plus_Expr  ( term_parse  ,  expr_parse ),
   tokens_after_expr))
```


Building Plus Expression Parse Tree

<expr> ::= <term> + <expr>

```
(match expr tokens_after_plus
  with ( expr_parse  , tokens_after_expr) ->
  ( Plus_Expr  ( term_parse  ,  expr_parse ),
   tokens_after_expr))
```

Parsing a Minus Expression

<expr> ::= <term> - <expr>

```
| ( Minus_token  :: tokens_after_minus) ->
   (match expr tokens_after_minus
   with ( expr_parse  , tokens_after_expr) ->
  ( Minus_Expr  ( term_parse  ,  expr_parse  ),
   tokens_after_expr))
```


Parsing a Minus Expression

<expr> ::= <term> - <expr>

```
| ( Minus_token  :: tokens_after_minus) ->
   (match expr tokens_after_minus
   with ( expr_parse  , tokens_after_expr) ->
  ( Minus_Expr  ( term_parse  ,  expr_parse  ),
   tokens_after_expr))
```


Parsing an Expression as a Term

<expr> ::= <term>

```
| _ -> (Term_as_Expr  term_parse  ,
  tokens_after_term)))
```

- Code for **term** is same except for replacing addition with multiplication and subtraction with division

Parsing Factor as Id

<factor> ::= <id>

```
and factor  tokens =
 (match tokens
  with (Id_token id_name :: tokens_after_id) =
   ( Id_as_Factor  id_name, tokens_after_id)
```


Parsing Factor as Parenthesized Expression

<factor> ::= (<expr>)

```
| factor ( Left_parenthesis  :: tokens) =
   (match expr tokens
    with ( expr_parse , tokens_after_expr) ->
```


Parsing Factor as Parenthesized Expression

<factor> ::= (<expr>)

```
(match tokens_after_expr
with Right_parenthesis :: tokens_after_rparen ->
 ( Parenthesized_Expr_as_Factor  expr_parse  ,
  tokens_after_rparen)
```

Error Cases

- What if no matching right parenthesis?

```
 | _ -> raise (Failure "No matching
rparen") ))
```

- What if no leading id or left parenthesis?

```
| _ -> raise (Failure "No id or lparen" ));;
```

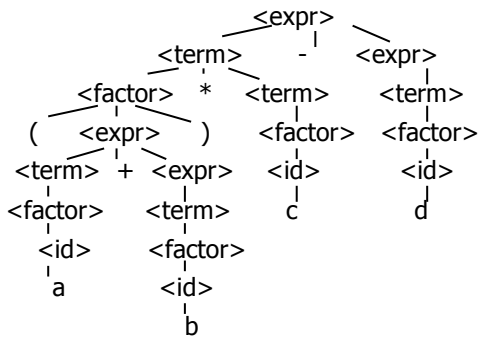

(a + b) * c - d

```
expr [Left_parenthesis; Id_token "a";
  Plus_token; Id_token "b";
  Right_parenthesis; Times_token;
  Id_token "c"; Minus_token;
  Id_token "d"];;
```


(a + b) * c - d

```
- : expr * token list =
(Minus_Expr
  (Mult_Term
    (Parenthesized_Expr_as_Factor
      (Plus_Expr
        (Factor_as_Term (Id_as_Factor "a"),
         Term_as_Expr (Factor_as_Term
  (Id_as_Factor "b")))),
    Factor_as_Term (Id_as_Factor "c")),
  Term_as_Expr (Factor_as_Term (Id_as_Factor
  "d"))),
 [])
```

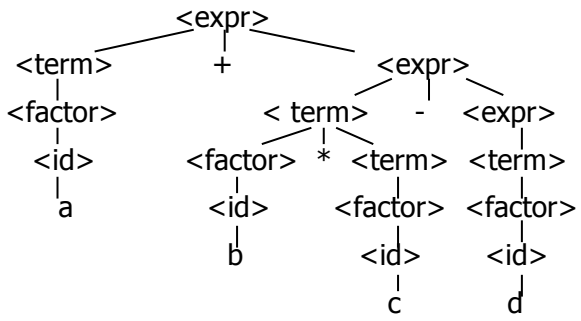

(a + b) * c – d



a + b * c – d

```
# expr [Id_token "a"; Plus_token; Id_token "b";
  Times_token; Id_token "c"; Minus_token;
       Id_token "d"];;
- : expr * token list =
(Plus_Expr
  (Factor_as_Term (Id_as_Factor "a"),
   Minus_Expr
    (Mult_Term (Id_as_Factor "b", Factor_as_Term
  (Id_as_Factor "c")),
     Term_as_Expr (Factor_as_Term (Id_as_Factor
  "d")))),
 [])
```


a + b * c – d



(a + b * c - d

```
# expr [Left_parenthesis; Id_token "a”;
Plus_token; Id_token "b”; Times_token;
Id_token "c”; Minus_token; Id_token "d"];;
```

Exception: Failure "No matching rparen".

Can’t parse because it was expecting a right parenthesis but it got to the end without finding one

a + b) * c – d (

```
expr [Id_token "a”; Plus_token; Id_token "b”;
  Right_parenthesis; Times_token; Id_token "c”;
  Minus_token; Id_token "d”; Left_parenthesis];;
- : expr * token list =
(Plus_Expr
 (Factor_as_Term (Id_as_Factor "a"),
  Term_as_Expr (Factor_as_Term (Id_as_Factor
  "b"))),
 [Right_parenthesis; Times_token; Id_token "c";
  Minus_token; Id_token "d"; Left_parenthesis])
```


Parsing Whole String

- Q: How to guarantee whole string parses?
- A: Check returned tokens empty

```
let parse tokens  =
   match expr tokens
    with (expr_parse, []) -> expr_parse
    | _ -> raise (Failure “No parse");;
```

- Fixes <expr> as start symbol

Streams in Place of Lists

- More realistically, we don't want to create the entire list of tokens before we can start parsing
- We want to generate one token at a time and use it to make one step in parsing
- Can use (token * (unit -> token)) or (token * (unit -> token option))
  in place of token list

Problems for Recursive-Descent Parsing

- Left Recursion:
  A ::= Aw
  translates to a subroutine that loops forever
- Indirect Left Recursion:
  A ::= Bw
  B ::= Av
  causes the same problem

Problems for Recursive-Descent Parsing

- Parser must always be able to choose the next action based only only the very next token
- Pairwise Disjointedness Test: Can we always determine which rule (in the non-extended BNF) to choose based on just the first token

Pairwise Disjointedness Test

- For each rule
  A ::= *y*

Calculate

FIRST (*y*) =
  {a | *y* =>* a*w*} ∪ {ε | if y =>* ε}

- For each pair of rules A ::= *y* and A ::= *z*, require FIRST(*y*) ∩ FIRST(*z*) = { }

Example

Grammar:
<S> ::= <A> a <B> b
<A> ::= <A> b | b
<B> ::= a <B> | a

FIRST (<A> b) = {b}
FIRST (b) = {b}
Rules for <A> not pairwise disjoint

Eliminating Left Recursion

- Rewrite grammar to shift left recursion to right recursion
  - Changes associativity
- Given

<expr> ::= <expr> + <term> and
<expr> ::= <term>

- Add new non-terminal <e> and replace above rules with

<expr> ::= <term><e>
<e> ::= + <term><e> | ε

Factoring Grammar

- Test too strong: Can't handle
  <expr> ::= <term> [(+ | -) <expr>]
- Answer: Add new non-terminal and replace above rules by
  <expr> ::= <term><e>
  <e> ::= + <term><e>
  <e> ::= - <term><e>
  <e> ::= ε
- You are delaying the decision point

Example

Both <A> and <B> have problems:

<S> ::= <A> a <B> b
<A> ::= <A> b | b
<B> ::= a <B> | a

Transform grammar to:

<S> ::= <A> a <B> b
<A> ::-= b<A1>
<A1> :: b<A1> | ε
<B> ::= a<B1>
<B1> ::= a<B1> | ε