

Programming Languages and Compilers (CS 421)

Elsa L Gunter
2112 SC, UIUC

<http://courses.engr.illinois.edu/cs421>

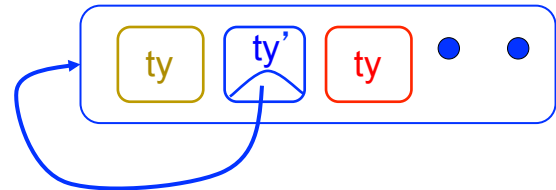
Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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Recursive Types

- The type being defined may be a component of itself



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Recursive Data Types

```
# type exp =  
  VarExp of string  
  | ConstExp of const  
  | MonOpAppExp of mon_op * exp  
  | BinOpAppExp of bin_op * exp * exp  
  | IfExp of exp * exp * exp  
  | AppExp of exp * exp  
  | FunExp of string * exp
```

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp  
  | EqOp | CommaOp | ConsOp | ...  
# type const = BoolConst of bool | IntConst of int | ...  
# type exp = VarExp of string | ConstExp of const  
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp  
  | EqOp | CommaOp | ConsOp | ...  
# type const = BoolConst of bool | IntConst of int | ...  
# type exp = VarExp of string | ConstExp of const  
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent 6 as an exp?
- Answer: ConstExp (IntConst 6)

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp  
  | EqOp | CommaOp | ConsOp | ...  
# type const = BoolConst of bool | IntConst of int | ...  
# type exp = VarExp of string | ConstExp of const  
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent (6, 3) as an exp?
- BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3))

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Recursive Data Types

```
# type bin_op = IntPlusOp | IntMinusOp
  | EqOp | CommaOp | ConsOp | ...
# type const = BoolConst of bool | IntConst of int |
...
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp | ...
```

- How to represent [(6, 3)] as an exp?
- BinOpAppExp (ConsOp, BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3)), ConstExp NilConst));;

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp
  | FunExp of string * exp | AppExp of exp * exp
```

- How to count the number of variables in an exp?

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp
  | FunExp of string * exp | AppExp of exp * exp
```

- How to count the number of variables in an exp?

```
# let rec varCnt exp =
  match exp with VarExp x ->
  | ConstExp c ->
  | BinOpAppExp (b, e1, e2) ->
  | FunExp (x,e) ->
  | AppExp (e1, e2) ->
```

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Recursion over Recursive Data Types

```
# type exp = VarExp of string | ConstExp of const
  | BinOpAppExp of bin_op * exp * exp
  | FunExp of string * exp | AppExp of exp * exp
# let rec varCnt exp =
  match exp with VarExp x -> 1
  | ConstExp c -> 0
  | BinOpAppExp (b, e1, e2) -> varCnt e1 + varCnt e2
  | FunExp (x,e) -> 1 + varCnt e
  | AppExp (e1, e2) -> varCnt e1 + varCnt e2
```

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Your turn now

Try Problem 3 on MP3

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Mutually Recursive Types

```
# type 'a tree = TreeLeaf of 'a
| TreeNode of 'a treeList
and 'a treeList = Last of 'a tree
| More of ('a tree * 'a treeList);;
type 'a tree = TreeLeaf of 'a | TreeNode of 'a
treeList
and 'a treeList = Last of 'a tree | More of ('a
tree * 'a treeList)
```

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Mutually Recursive Types - Values

```
# let tree =
  TreeNode
  (More (TreeLeaf 5,
        (More (TreeNode
              (More (TreeLeaf 3,
                    Last (TreeLeaf 2))),
                Last (TreeLeaf 7)))));;
```

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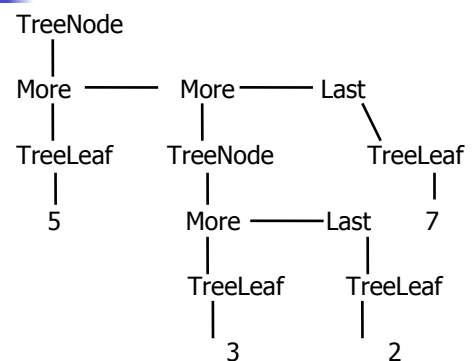
Mutually Recursive Types - Values

```
val tree : int tree =
  TreeNode
  (More
   (TreeLeaf 5,
    More
     (TreeNode (More (TreeLeaf 3, Last
                     (TreeLeaf 2))), Last (TreeLeaf 7))))
```

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Mutually Recursive Types - Values

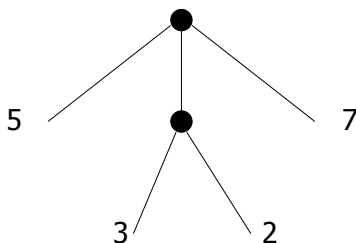


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Mutually Recursive Types - Values

A more conventional picture



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Mutually Recursive Functions

```
# let rec fringe tree =
  match tree with (TreeLeaf x) -> [x]
| (TreeNode list) -> list_fringe list
and list_fringe tree_list =
  match tree_list with (Last tree) -> fringe tree
| (More (tree,list)) ->
  (fringe tree) @ (list_fringe list);;
```

```
val fringe : 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>
```

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Mutually Recursive Functions

```
# fringe tree;;  
- : int list = [5; 3; 2; 7]
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;  
Define tree_size
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;  
Define tree_size  
let rec tree_size t =  
  match t with TreeLeaf _ ->  
  | TreeNode ts ->
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;  
Define tree_size  
let rec tree_size t =  
  match t with TreeLeaf _ -> 1  
  | TreeNode ts -> treeList_size ts
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;  
Define tree_size and treeList_size  
let rec tree_size t =  
  match t with TreeLeaf _ -> 1  
  | TreeNode ts -> treeList_size ts  
and treeList_size ts =
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList  
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;  
Define tree_size and treeList_size  
let rec tree_size t =  
  match t with TreeLeaf _ -> 1  
  | TreeNode ts -> treeList_size ts  
and treeList_size ts =  
  match ts with Last t ->  
  | More t ts' ->
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
  match ts with Last t -> tree_size t
  | More t ts' -> tree_size t + treeList_size ts'
```

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Problem

```
# type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);;
Define tree_size and treeList_size
let rec tree_size t =
  match t with TreeLeaf _ -> 1
  | TreeNode ts -> treeList_size ts
and treeList_size ts =
  match ts with Last t -> tree_size t
  | More t ts' -> tree_size t + treeList_size ts'
```

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Nested Recursive Types

```
# type 'a labeled_tree =
  TreeNode of ('a * 'a labeled_tree
  list);;
type 'a labeled_tree = TreeNode of ('a
  * 'a labeled_tree list)
```

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Nested Recursive Type Values

```
# let ltree =
  TreeNode(5,
  [TreeNode (3, []);
  TreeNode (2, [TreeNode (1, []);
  TreeNode (7, [])]);
  TreeNode (5, [])]);;
```

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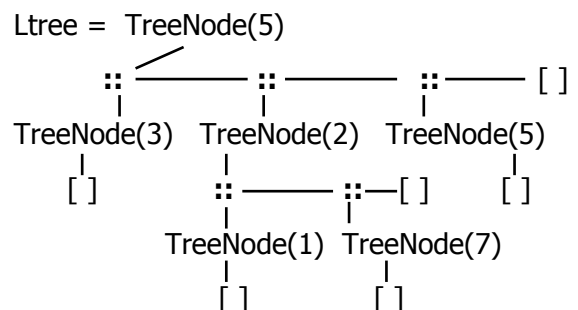
Nested Recursive Type Values

```
val ltree : int labeled_tree =
  TreeNode
  (5,
  [TreeNode (3, []); TreeNode (2,
  [TreeNode (1, []); TreeNode (7, [])]);
  TreeNode (5, [])])
```

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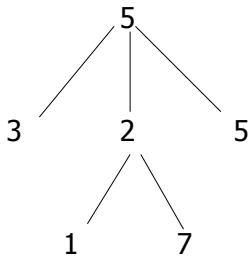
Nested Recursive Type Values



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Nested Recursive Type Values



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Mutually Recursive Functions

```
# let rec flatten_tree labtree =  
  match labtree with TreeNode (x,treelist)  
  -> x::flatten_tree_list treelist  
and flatten_tree_list treelist =  
  match treelist with [] -> []  
  | labtree::labtrees  
  -> flatten_tree labtree  
  @ flatten_tree_list labtrees;;
```

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Mutually Recursive Functions

```
val flatten_tree : 'a labeled_tree -> 'a list =  
  <fun>  
val flatten_tree_list : 'a labeled_tree list -> 'a  
  list = <fun>  
# flatten_tree ltree;;  
- : int list = [5; 3; 2; 1; 7; 5]
```

- Nested recursive types lead to mutually recursive functions

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Infinite Recursive Values

```
# let rec ones = 1::ones;;  
val ones : int list =  
  [1; 1; 1; 1; ...]  
# match ones with x::_ -> x;;  
Characters 0-25:  
Warning: this pattern-matching is not exhaustive.  
Here is an example of a value that is not matched:  
[]  
  match ones with x::_ -> x;;  
  ^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^  
- : int = 1
```

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Infinite Recursive Values

```
# let rec lab_tree = TreeNode(2, tree_list)  
  and tree_list = [lab_tree; lab_tree];;  
val lab_tree : int labeled_tree =  
  TreeNode (2, [TreeNode(...); TreeNode(...)])  
val tree_list : int labeled_tree list =  
  [TreeNode (2, [TreeNode(...);  
  TreeNode(...)]);  
  TreeNode (2, [TreeNode(...);  
  TreeNode(...)])]
```

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Infinite Recursive Values

```
# match lab_tree  
  with TreeNode (x, _) -> x;;  
- : int = 2
```

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Records

- Records serve the same programming purpose as tuples
- Provide better documentation, more readable code
- Allow components to be accessed by label instead of position
 - Labels (aka *field names*) must be unique
 - Fields accessed by suffix dot notation

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Record Types

- Record types must be declared before they can be used in OCaml

```
# type person = {name : string; ss : (int * int * int); age : int};;
```

```
type person = { name : string; ss : int * int * int; age : int; }
```

- person is the type being introduced
- name, ss and age are the labels, or fields

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Record Values

- Records built with labels; order does not matter

```
# let teacher = {name = "Elsa L. Gunter"; age = 102; ss = (119,73,6244)};;  
val teacher : person =  
  {name = "Elsa L. Gunter"; ss = (119, 73, 6244); age = 102}
```

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Record Pattern Matching

```
# let {name = elsa; age = age; ss = (_,_,s3)} = teacher;;
```

```
val elsa : string = "Elsa L. Gunter"
```

```
val age : int = 102
```

```
val s3 : int = 6244
```

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Record Field Access

```
# let soc_sec = teacher.ss;;  
val soc_sec : int * int * int = (119, 73, 6244)
```

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Record Values

```
# let student = {ss=(325,40,1276); name="Joseph Martins"; age=22};;
```

```
val student : person =
```

```
  {name = "Joseph Martins"; ss = (325, 40, 1276); age = 22}
```

```
# student = teacher;;
```

```
- : bool = false
```

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New Records from Old

```
# let birthday person = {person with age =  
  person.age + 1};;  
val birthday : person -> person = <fun>  
# birthday teacher;;  
- : person = {name = "Elsa L. Gunter"; ss =  
  (119, 73, 6244); age = 103}
```

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New Records from Old

```
# let new_id name soc_sec person =  
  {person with name = name; ss = soc_sec};;  
val new_id : string -> int * int * int -> person  
  -> person = <fun>  
# new_id "Guiesepe Martin" (523,04,6712)  
  student;;  
- : person = {name = "Guiesepe Martin"; ss  
  = (523, 4, 6712); age = 22}
```

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