Programming Languages and Compilers (CS 421)



Elsa L Gunter 2112 SC, UIUC



http://courses.engr.illinois.edu/cs421

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

Dennis Griffith, guest lecturer

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> ■ Tuesday 12:00pm - 1:30pm ■ Thursday 3:30pm - 4:20pm

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Overflow Section

- If you are not registered and want to be, fill out the form at
- http://go.cs.illinois.edu/CS421Overflow

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Course TAs



Susannah Johnson



John Lee



Terence Nip



Michael Bay

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Contact Information - TAs

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■ Hours: Mon 12:00pm - 12:50pm Fri 10:00am - 10:50am

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Hours: Tues 4:00pm – 4:50pm Thurs 11:15am - 12:05am

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Hours: Fri 4:00pm – 5:45pm

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Course Website

- http://courses.engr.illinois.edu/cs421
- Main page summary of news items
- Policy rules governing course
- Lectures syllabus and slides
- MPs information about assignments
- Exams
- Unit Projects for 4 credit students
- Resources tools and helpful info
- FAQ

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Some Course References

- No required textbook
- Some suggested references







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Some Course References

- No required textbook.
- Pictures of the books on previous slide
- Essentials of Programming Languages (2nd Edition) by Daniel P. Friedman, Mitchell Wand and Christopher T. Haynes, MIT Press 2001.
- Compilers: Principles, Techniques, and Tools, (also known as "The Dragon Book"); by Aho, Sethi, and Ullman. Published by Addison-Wesley. ISBN: 0-201-10088-6.
- Modern Compiler Implementation in ML by Andrew W. Appel, Cambridge University Press 1998
- Additional ones for Ocaml given separately

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Course Grading

- Assignments 20%
 - About 12 Hand Written (HW) assignments (~7%)
 - About 8 MPs (in Ocaml) (~7%)
 - About 4 Labs (~6%)
 - All HW and MPs Submitted by svn
 - MPs plain text code that compiles; HWs pdf
 - Late submission penalty: 20% of assignments total value
 - Labs in Computer-Based Testing Center (DCL)
 - Self-scheduled over a three day period
 - No extensions beyond the three day period
 - Fall back: Labs bécome MPs

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Course Grading

- 2 Midterms 20% each
 - Labs in Computer-Based Testing Center (DCL)
 - Self-scheduled over a three day period
 - No extensions beyond the three day period
 - Fall back: In class backup dates Oct 8, Nov 11
 - DO NOT MISS EXAM DATES!
- Final 40% Dec 16, 8:00am 11:00am
- Will investigate use of CBTC for Final
- Percentages are approximate



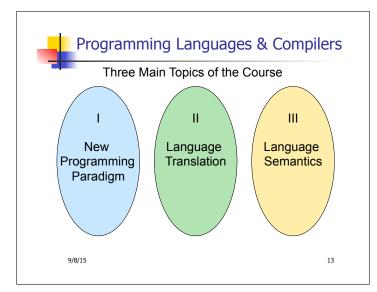
Course Assingments – Handwritten & MP

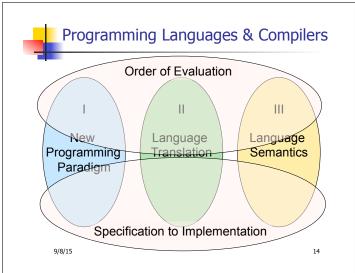
- You may discuss assignments and their solutions with others
- You may work in groups, but you must list members with whom you worked if you share solutions or solution outlines
- Each student must write up and turn in their own solution separately
- You may look at examples from class and other similar examples from any source – cite appropriately
 - Note: University policy on plagiarism still holds cite your sources if you are not the sole author of your solution

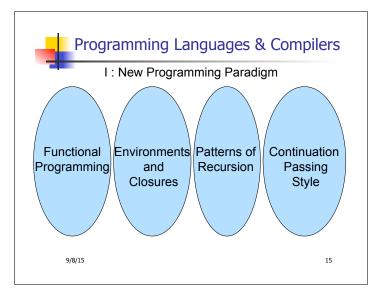
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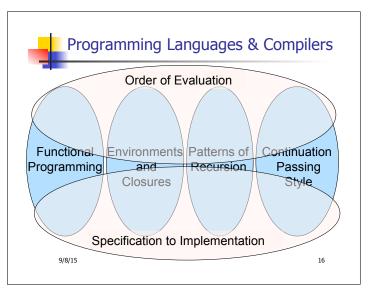
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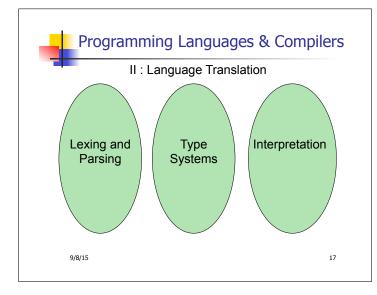
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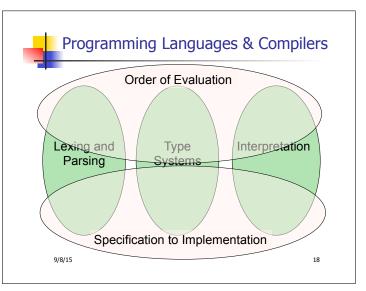


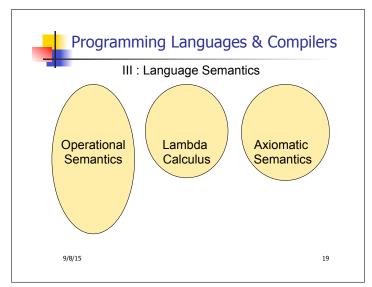


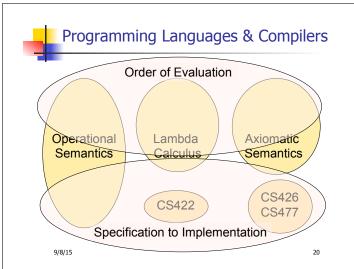














Course Objectives

- New programming paradigm
 - Functional programming
 - Environments and Closures
 - Patterns of Recursion
 - Continuation Passing Style
- Phases of an interpreter / compiler
 - Lexing and parsing
 - Type systems
 - Interpretation
- Programming Language Semantics
 - Lambda Calculus
 - Operational Semantics
 - Axiomatic Semantics

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- Locally:
 - Compiler is on the EWS-linux systems at /usr/local/bin/ocaml
- Globally:
 - Main CAML home: http://ocaml.org
 - To install OCAML on your computer see: http://ocaml.org/docs/install.html

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References for OCaml

- Supplemental texts (not required):
- The Objective Caml system release 4.02, by Xavier Leroy, online manual
- Introduction to the Objective Caml Programming Language, by Jason Hickey
- Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O' Reilly
 - Available online from course resources

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OCAML Background

- CAML is European descendant of original ML
 - American/British version is SML
 - O is for object-oriented extension
- ML stands for Meta-Language
- ML family designed for implementing theorem provers
 - It was the meta-language for programming the "object" language of the theorem prover
 - Despite obscure original application area, OCAML is a full general-purpose programming language



Features of OCAML

- Higher order applicative language
- Call-by-value parameter passing
- Modern syntax
- Parametric polymorphism
 - Aka structural polymorphism
- Automatic garbage collection
- User-defined algebraic data types
- It's fast winners of the 1999 and 2000 ICFP Programming Contests used OCAML

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Why learn OCAML?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCAML is particularly efficient for programming tasks involving languages (eg parsing, compilers, user interfaces)
- Industrially Relevant: Jane Street trades billions of dollars per day using OCaml programs
- Similar languages: Microsoft F#, SML, Haskell, Scala

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OCaml Intro Code

- A (possibly better, non-PowerPoint) text version of this lecture can be found at http://course.engr.illinois.edu/class/cs421/lectures/ocaml-intro-shell.txt
- For the OCAML code for today's lecture see
 - http://course.engr.illinois.edu/class/cs421/ lectures/ocaml-intro.ml

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Session in OCAML

% ocaml

Objective Caml version 4.01

(* Read-eval-print loop; expressions and declarations *)

2 + 3;; (* Expression *)

: int = 5

3 < 2;;

- : bool = false

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No Overloading for Basic Arithmetic Operations

```
# 15 * 2;;
-: int = 30
# 1.35 + 0.23;; (* Wrong type of addition *)
Characters 0-4:
   1.35 + 0.23;; (* Wrong type of addition *)
   ^^^<
Error: This expression has type float but an expression was expected of type int</pre>
```

1.35 +. 0.23;; -: float = 1.58

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No Implicit Coercion

```
# 1.0 * 2;; (* No Implicit Coercion *)
Characters 0-3:
1.0 * 2;; (* No Implicit Coercion *)
^^
```

Error: This expression has type float but an expression was expected of type int

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```
1
```

Sequencing Expressions

```
# "Hi there";; (* has type string *)
-: string = "Hi there"
# print_string "Hello world\n";; (* has type unit *)
Hello world
-: unit = ()
# (print_string "Bye\n"; 25);; (* Sequence of exp *)
Bye
-: int = 25
```

```
Declarations; Sequencing of Declarations

# let x = 2 + 3;; (* declaration *)

val x : int = 5

# let test = 3 < 2;;

val test : bool = false

# let a = 1 let b = a + 4;; (* Sequence of dec *)

val a : int = 1

val b : int = 5
```



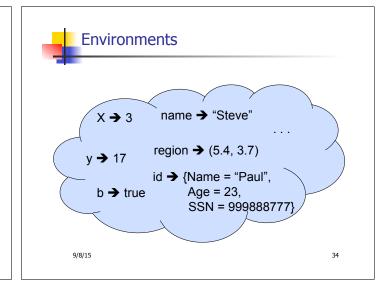
Environments

- Environments record what value is associated with a given identifier
- Central to the semantics and implementation of a language
- Notation

 $\rho = \{ name_1 \rightarrow value_1, name_2 \rightarrow value_2, ... \}$ Using set notation, but describes a partial function

- Often stored as list, or stack
 - To find value start from left and take first match

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Global Variable Creation

```
# 2 + 3;; (* Expression *)

// doesn' t affect the environment

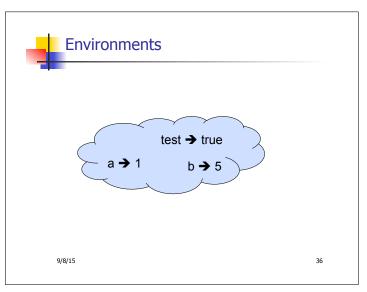
# let test = 3 < 2;; (* Declaration *)

val test : bool = false

// \rho_1 = {test \rightarrow false}

# let a = 1 let b = a + 4;; (* Seq of dec *)

// \rho_2 = {b \rightarrow 5, a \rightarrow 1, test \rightarrow false}
```





New Bindings Hide Old

//
$$\rho_2 = \{b \rightarrow 5, a \rightarrow 1, \text{ test} \rightarrow \text{ false}\}\$$
 let test = 3.7;;

What is the environment after this declaration?

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New Bindings Hide Old

//
$$\rho_2 = \{b \rightarrow 5, a \rightarrow 1, \text{ test } \rightarrow \text{ false}\}\$$
let test = 3.7;;

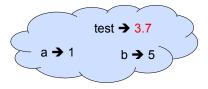
What is the environment after this declaration?

//
$$\rho_3 = \{ \text{test} \to 3.7, \, a \to 1, \, b \to 5 \}$$

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Environments



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Now it's your turn

You should be able to do HW1

Problem 1, parts (* 1 *) and (* 2 *)

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Local Variable Creation

```
// \rho_3 = \{\text{test} \to 3.7, \, a \to 1, \, b \to 5\}
# let b = 5 * 4

// \rho_4 = \{b \to 20, \, \text{test} \to 3.7, \, a \to 1\}
in 2 * b;;
-: int = 40

// \rho_5 = \rho_3 = \{\text{test} \to 3.7, \, a \to 1, \, b \to 5\}
# b;;
-: int = 5
```

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Local let binding

```
// \rho_5 = {test \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5}
# let c =
let b = a + a
// \rho_6 = {b \rightarrow 2} + \rho_3
// ={b \rightarrow 2, test \rightarrow 3.7, a \rightarrow 1}
in b * b;;
val c : int = 4
// \rho_7 = {c \rightarrow 4, test \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5}
# b;;
- : int = 5
```

```
Local let binding

// \rho_5 = \{\text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1, \, \text{b} \rightarrow 5\}

# let c =

let b = a + a

// \rho_6 = \{\text{b} \rightarrow 2\} + \rho_3

// = \{\text{b} \rightarrow 2, \, \text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1\}

in b * b;

val c : \text{int} = 4

// \rho_7 = \{\text{c} \rightarrow 4, \, \text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1, \, \text{b} \rightarrow 5\}

# b;;

-: int = 5
```

```
Local let binding

// \rho_5 = \{\text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1, \, \text{b} \rightarrow 5\}

# let c = \text{let b} = \text{a} + \text{a}

// \rho_6 = \{\text{b} \rightarrow 2\} + \text{p}

= \{\text{b} \rightarrow 2, \, \text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1\}

in \text{b} * \text{b}_{//}

val c : \text{int} = 4

// \rho_7 = \{\text{c} \rightarrow 4, \, \text{test} \rightarrow 3.7, \, \text{a} \rightarrow 1, \, \text{b} \rightarrow 5\}

# b;;

-: int = 5
```



Now it's your turn

You should be able to do HW1

Problem 1, parts (* 3 *) and (* 4 *)

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```
Booleans (aka Truth Values)

# true;;
-: bool = true

# false;;
-: bool = false

// \rho_7 = \{c \rightarrow 4, \text{ test} \rightarrow 3.7, \text{ a} \rightarrow 1, \text{ b} \rightarrow 5\}

# if b > a then 25 else 0;;
-: int = 25
```



Booleans and Short-Circuit Evaluation

```
# 3 > 1 && 4 > 6;;
-: bool = false
# 3 > 1 || 4 > 6;;
-: bool = true
# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
Hi
-: bool = true
# 3 > 1 || (print_string "Bye\n"; 4 > 6);;
-: bool = true
# not (4 > 6);;
-: bool = true
```



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Now it's your turn

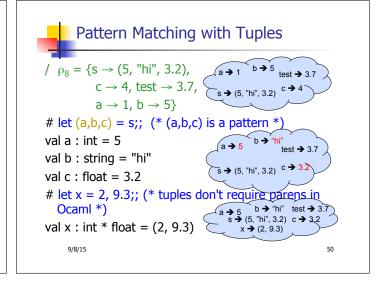
You should be able to do HW1 Problem 1, part (* 5 *)

// 0-

Tuples as Values

```
// \rho_7 = \{c \to 4, \text{ test} \to 3.7, \\ a \to 1, b \to 5\}
# let s = (5, \text{"hi"}, 3.2);
val s : \text{int * string * float } = (5, \text{"hi"}, 3.2)

// \rho_8 = \{s \to (5, \text{"hi"}, 3.2), \\ c \to 4, \text{ test} \to 3.7, \\ a \to 1, b \to 5\}
```





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Nested Tuples

```
# (*Tuples can be nested *)
let d = ((1,4,62),("bye",15),73.95);;
val d : (int * int * int) * (string * int) * float =
        ((1,4,62), ("bye", 15), 73.95)
# (*Patterns can be nested *)
let (p,(st,_),_) = d;; (* _ matches all, binds nothing
        *)
val p : int * int * int = (1, 4, 62)
val st : string = "bye"
```

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Now it's your turn

You should be able to do HW1 Problem 1, part (* 6 *)

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Functions

```
# let plus_two n = n + 2;;
val plus_two : int -> int = <fun>
# plus_two 17;;
- : int = 19
```

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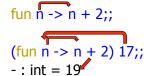
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Functions



Nameless Functions (aka Lambda Terms)







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Functions

```
# let plus_two n = n + 2;;
val plus_two : int -> int = <fun>
# plus_two 17;;
- : int = 19
# let plus_two = fun n -> n + 2;;
val plus_two : int -> int = <fun>
# plus_two 14;;
- : int = 16
```

First definition syntactic sugar for second

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Using a nameless function

Note: in fun v -> exp(v), scope of variable is only the body exp(v)

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Values fixed at declaration time

What is the result?

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Values fixed at declaration time

```
# let x = 12;;
val x : int = 12
# let plus_x y = y + x;;
val plus_x : int -> int = <fun>
# plus_x 3;;
- : int = 15
```

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Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an
update *)
val x : int = 7
# plus_x 3;;
```

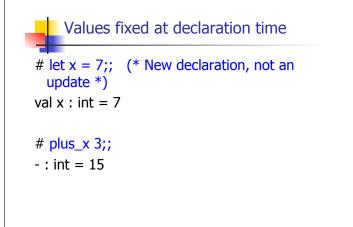
What is the result this time?



Values fixed at declaration time

What is the result this time?

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Question

- Observation: Functions are first-class values in this language
- Question: What value does the environment record for a function variable?
- Answer: a closure

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Save the Environment!

 A closure is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:

$$f \rightarrow \langle (v1,...,vn) \rightarrow exp, \rho_f \rangle$$

Where ρ_f is the environment in effect when f is defined (if f is a simple function)

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Closure for plus x

When plus_x was defined, had environment:

$$\rho_{\text{plus}_x} = \{..., x \rightarrow 12, ...\}$$

- Recall: let plus_x y = y + x is really let plus x = fun y -> y + x
- Closure for fun y -> y + x:

$$\langle y \rightarrow y + x, \rho_{\text{plus } x} \rangle$$

• Environment just after plus_x defined:

$$\{plus_x \rightarrow \langle y \rightarrow y + x, \rho_{plus_x} \rangle\} + \rho_{plus_x}$$

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Now it's your turn

You should be able to do HW1 Problem 1 , parts (* 7 *) and (* 8 *)



Evaluation of Application of plus_x;;

Have environment:

```
\begin{split} \rho = \{ plus\_x \rightarrow <& y \rightarrow y + x, \, \rho_{plus\_x} >, \, ... \,, \\ y \rightarrow & 3, \, ... \} \end{split}
```

where $\rho_{\text{plus } x} = \{x \rightarrow 12, ..., y \rightarrow 24, ...\}$

- Eval (plus_x y, ρ) rewrites to
- Eval (App $\langle y \rightarrow y + x, \rho_{plus} \rangle > 3, \rho$) rewrites to
- Eval (y + x, {y \rightarrow 3} + ρ_{plus_x}) rewrites to
- Eval $(3 + 12, \rho_{\text{plus } x}) = 15$

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Functions with more than one argument

```
# let add_three x y z = x + y + z;;
val add_three : int -> int -> int -> int = <fun>
# let t = add_three 6 3 2;;
val t : int = 11
# let add_three =
fun x -> (fun y -> (fun z -> x + y + z));;
val add_three : int -> int -> int -> int = <fun>
```

Again, first syntactic sugar for second

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Partial application of functions

let add_three x y z = x + y + z;;

```
# let h = add_three 5 4;;
val h : int -> int = <fun>
# h 3;;
- : int = 12
# h 7;;
- : int = 16
```

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Functions as arguments

```
# let thrice f x = f (f (f x));;
val thrice : ('a -> 'a) -> 'a -> 'a = <fun>
# let g = thrice plus_two;;
val g : int -> int = <fun>
# g 4;;
- : int = 10
# thrice (fun s -> "Hi! " ^ s) "Good-bye!";;
- : string = "Hi! Hi! Hi! Good-bye!"
```

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Functions on tuples

```
# let plus_pair (n,m) = n + m;;

val plus_pair : int * int -> int = <fun>
# plus_pair (3,4);;

-: int = 7
# let double x = (x,x);;

val double : 'a -> 'a * 'a = <fun>
# double 3;;

-: int * int = (3, 3)
# double "hi";;

-: string * string = ("hi", "hi")

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```



Match Expressions

let triple_to_pair triple =

```
match triple
with (0, x, y) -> (x, y)
| (x, 0, y) -> (x, y)
| (x, y, _) -> (x, y);;
```

 Each clause: pattern on left, expression on right

•Each x, y has scope of only its clause

Use first matching clause

val triple_to_pair : int * int * int -> int * int =
 <fun>



Closure for plus_pair

- Assume ρ_{plus_pair} was the environment just before plus_pair defined
- Closure for plus_pair:

$$<$$
(n,m) \rightarrow n + m, $\rho_{plus_pair}>$

Environment just after plus_pair defined:

{plus_pair
$$\rightarrow$$
 <(n,m) \rightarrow n + m, ρ_{plus_pair} >}
+ ρ_{plus_pair}

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Evaluation of Application with Closures

- In environment ρ , evaluate left term to closure, $c = \langle (x_1,...,x_n) \rightarrow b, \rho \rangle$
- (x₁,...,x_n) variables in (first) argument
- Evaluate the right term to values, (v₁,...,v_n)
- Update the environment ρ to

$$\rho' = \{x_1 \to v_1, ..., x_n \to v_n\} + \rho$$

Evaluate body b in environment ρ'

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Evaluation of Application of plus_pair

Assume environment

$$\rho = \{x \rightarrow 3..., \\ plus_pair \rightarrow <(n,m) \rightarrow n + m, \rho_{plus_pair}>\} + \\ \rho_{plus_pair}$$

- Eval (plus_pair (4,x), ρ)=
- Eval (App <(n,m) \rightarrow n + m, $\rho_{\text{plus_pair}}>$ (4,x), ρ)) =
- Eval (App <(n,m) \rightarrow n + m, $\rho_{\text{plus pair}}$ > (4,3), ρ)) =
- Eval (n + m, {n -> 4, m -> 3} + ρ_{plus_pair}) =
- Eval $(4 + 3, \{n -> 4, m -> 3\} + \rho_{plus_pair}) = 7$

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Closure question

If we start in an empty environment, and we execute:

What is the environment at (* 0 *)?

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Answer

$$\rho_0 = \{f \to \langle n \to n + 5, \{ \} \rangle \}$$



Closure question

• If we start in an empty environment, and we execute:

```
let f = fun => n + 5;;
let pair_map g (n,m) = (g n, g m);;
(* 1 *)
let f = pair_map f;;
```

What is the environment at (*1*)?

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```
Answer

\rho_0 = \{f \to < n \to n + 5, \{ \} > \} \\
\text{let pair_map g (n,m) = (g n, g m);;}

\rho_1 = \{\text{pair_map} \to \\
< g \to \text{fun (n,m)} \to (g n, g m), \\
& \{f \to < n \to n + 5, \{ \} > \} >, \\
& f \to < n \to n + 5, \{ \} > \}
```

Closure question

• If we start in an empty environment, and we execute:

```
let f = fun => n + 5;;
let pair_map g (n,m) = (g n, g m);;
let f = pair_map f;;
(* 2*)
```

What is the environment at (* 2 *)?

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Answer



Recall

val add_three : int -> int -> int -> int = <fun>

How does it differ from

let add_triple (u,v,w) = u + v + w;;
val add_triple : int * int * int -> int = <fun>

- add_three is curried;
- add triple is uncurried

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Curried vs Uncurried



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Scoping Question

Consider this code:

```
let x = 27;;
let f x =
let x = 5 in
(fun x -> print_int x) 10;;
f 12;;
```

What value is printed?

5 10

10 12

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