

Unary Primitive Operators:

$$\frac{\Gamma \vdash e : \tau_1}{\Gamma \vdash \odot e : \tau_2} \text{ MONOP} \quad \tau_1 \rightarrow \tau_2 \text{ an instance of } \text{sig}(\odot).$$

Binary Primitive Operators:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash e_1 \odot e_2 : \tau_3} \text{ BINOP} \quad \tau_1 \rightarrow \tau_2 \rightarrow \tau_3 \text{ an instance of } \text{sig}(\odot).$$

If-then-else rule:

$$\frac{\Gamma \vdash e_c : \text{bool} \quad \Gamma \vdash e_t : \tau \quad \Gamma \vdash e_e : \tau}{\Gamma \vdash \text{if } e_c \text{ then } e_t \text{ else } e_e : \tau} \text{ IF}$$

Application rule:

$$\frac{\Gamma \vdash e_1 : \tau_1 \rightarrow \tau_2 \quad \Gamma \vdash e_2 : \tau_1}{\Gamma \vdash e_1 e_2 : \tau_2} \text{ APP}$$

Function rule:

$$\frac{[x : \tau_1] + \Gamma \vdash e : \tau_2}{\Gamma \vdash \text{fun } x \rightarrow e : \tau_1 \rightarrow \tau_2} \text{ FUN}$$

Let rule:

$$\frac{\Gamma \vdash e_1 : \tau_1 \quad [x : \text{Gen}(\tau_1, \Gamma)] + \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 : \tau_2} \text{ LET}$$

Let Rec rule:

$$\frac{[x : \tau_1] + \Gamma \vdash e_1 : \tau_1 \quad [x : \text{Gen}(\tau_1, \Gamma)] + \Gamma \vdash e_2 : \tau_2}{\Gamma \vdash \text{let rec } x = e_1 \text{ in } e_2 : \tau_2} \text{ REC}$$

$\text{Gen}(\tau, \Gamma) = \forall \alpha_1 \dots \alpha_n. \tau$ where $\alpha_1, \dots, \alpha_n$ are the type variables that occur in τ but do not occur free in Γ .