Programming Languages and Compilers (CS 421)

Elsa L Gunter 2112 SC, UIUC

http://www.cs.uiuc.edu/class/cs421/

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

CPS Transformation

- Step 1: Add continuation argument to any function definition:
 - let f arg = e \Rightarrow let f arg k = e
 - Idea: Every function takes an extra parameter saying where the result goes
- Step 2: A simple expression in tail position should be passed to a continuation instead of returned:
 - return $a \Rightarrow k a$
 - Assuming a is a constant or variable.
 - "Simple" = "No available function calls."

CPS Transformation

- Step 3: Pass the current continuation to every function call in tail position
 - return f arg₁ ... arg_n \Rightarrow f arg₁ ... arg_n k
 - The function "isn't going to return," so we need to tell it where to put the result.

CPS Transformation

- Step 4: Each function call not in tail position needs to be built into a new continuation (containing the old continuation as appropriate)
 - return op (f arg) \Rightarrow f arg (fun r -> k(op r))
 - op represents a primitive operation
 - return $f(g arg) \Rightarrow g arg (fun r-> f r k)$

Example

Before:

let rec add_list lst = match lst with

```
[]-> 0
| 0 :: xs -> add_list xs
| x :: xs -> (+) x
   (add_list xs);;
```

After:

Other Uses for Continuations

- CPS designed to preserve order of evaluation
- Continuations used to express order of evaluation
- Can be used to change order of evaluation
- Implements:
 - Exceptions and exception handling
 - Co-routines
 - (pseudo) threads

Exceptions - Example

exception Zero;; exception Zero # let rec list mult aux list = match list with $[] \rightarrow 1$ | X ::: XS -> if x = 0 then raise Zero else x * list mult aux xs;; val list mult aux : int list -> int = <fun>

Exceptions - Example

let list_mult list =

try list_mult_aux list with Zero -> 0;;
val list_mult : int list -> int = <fun>
list_mult [3;4;2];;

- -: int = 24
- # list_mult [7;4;0];;
- -: int = 0
- # list_mult_aux [7;4;0];;
 Exception: Zero.

Exceptions

- When an exception is raised
 - The current computation is aborted
 - Control is "thrown" back up the call stack until a matching handler is found
 - All the intermediate calls waiting for a return value are thrown away

Implementing Exceptions

```
# let multkp m n k =
  let r = m * n in
   (print_string "product result: ";
   print int r; print string "\n";
   k r);;
val multkp : int -> int -> (int -> 'a) -> 'a
 = < fun >
```

Implementing Exceptions

let rec list_multk_aux list k kexcp = match list with $[] \rightarrow k 1$ $| x :: xs \rightarrow if x = 0$ then kexcp 0 else list_multk_aux xs (fun r -> multkp x r k) kexcp;; val list_multk_aux : int list -> (int -> 'a) -> (int -> 'a) -> 'a = <fun> # let rec list multk list k = list multk aux list k k;;

val list_multk : int list -> (int -> 'a) -> 'a = <fun>

Implementing Exceptions

```
# list_multk [3;4;2] report;;
product result: 2
product result: 8
product result: 24
24
-: unit = ()
# list_multk [7;4;0] report;;
```

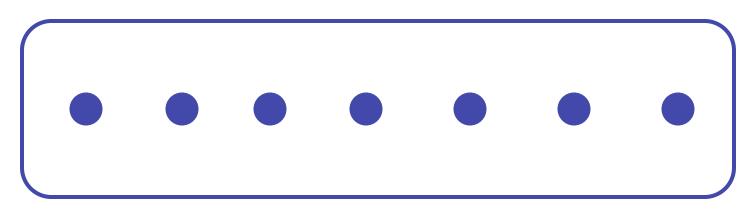
0

Variants - Syntax (slightly simplified)

- type $name = C_1 [of ty_1] | ... | C_n [of ty_n]$
- Introduce a type called name
- (fun x -> C_i x) : ty₁ -> name
- *C_i* is called a *constructor*; if the optional type argument is omitted, it is called a *constant*
- Constructors are the basis of almost all pattern matching



An enumeration type is a collection of distinct values



In C and Ocaml they have an order structure; order by order of input

Enumeration Types as Variants

type weekday = Monday | Tuesday | Wednesday Thursday | Friday | Saturday | Sunday;; type weekday = Monday | Tuesday | Wednesday | Thursday | Friday Saturday

| Sunday

Functions over Enumerations

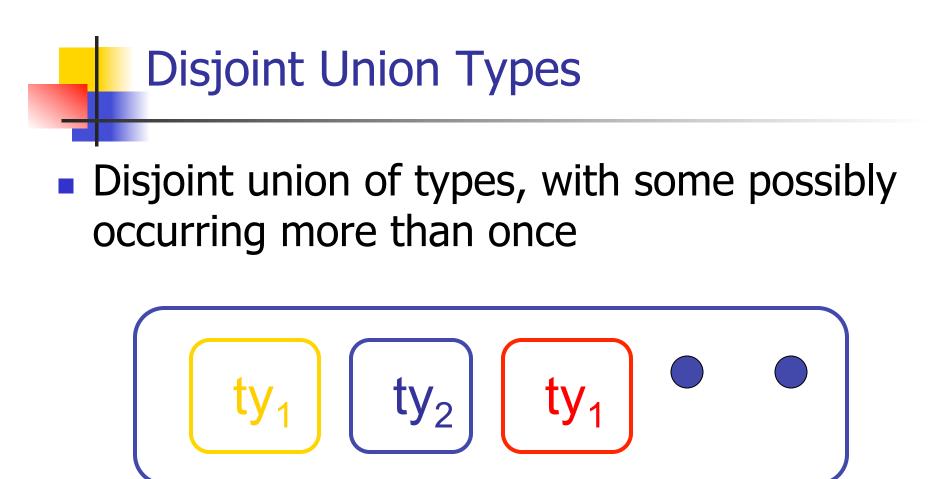
let day_after day = match day with Monday -> Tuesday **Tuesday** -> Wednesday Wednesday -> Thursday Thursday -> Friday Friday -> Saturday Saturday -> Sunday Sunday -> Monday;; val day after : weekday -> weekday = <fun>

Functions over Enumerations

let rec days_later n day = match n with 0 -> day -> if n > 0 then day_after (days_later (n - 1) day) else days_later (n + 7) day;; val days later : int -> weekday -> weekday = < fun >

Functions over Enumerations

- # days_later 2 Tuesday;;
- : weekday = Thursday
- # days_later (-1) Wednesday;;
- : weekday = Tuesday
- # days_later (-4) Monday;;
- : weekday = Thursday



We can also add in some new singleton elements

Disjoint Union Types

type id = DriversLicense of int SocialSecurity of int | Name of string;; type id = DriversLicense of int | SocialSecurity of int | Name of string # let check id id = match id with DriversLicense num -> not (List.mem num [13570; 99999]) SocialSecurity num -> num < 900000000 | Name str -> not (str = "John Doe");; val check id : id -> bool = <fun>



The type 'a option is gives us something to represent non-existence or failure

type 'a option = Some of 'a | None;;
type 'a option = Some of 'a | None

Used to encode partial functions
Often can replace the raising of an exception

Functions over option

let rec first p list =
 match list with [] -> None
 | (x::xs) -> if p x then Some x else first p xs;;
val first : ('a -> bool) -> 'a list -> 'a option = <fun>
first (fun x -> x > 3) [1;3;4;2;5];;
- : int option = Some 4

- # first (fun x -> x > 5) [1;3;4;2;5];;
- : int option = None

Mapping over Variants

let optionMap f opt = match opt with None -> None | Some $x \rightarrow$ Some (f x);; val optionMap : (a -> b) -> a option -> boption = <fun> # optionMap (fun x -> x - 2)(first (fun x -> x > 3) [1;3;4;2;5]);;

-: int option = Some 2

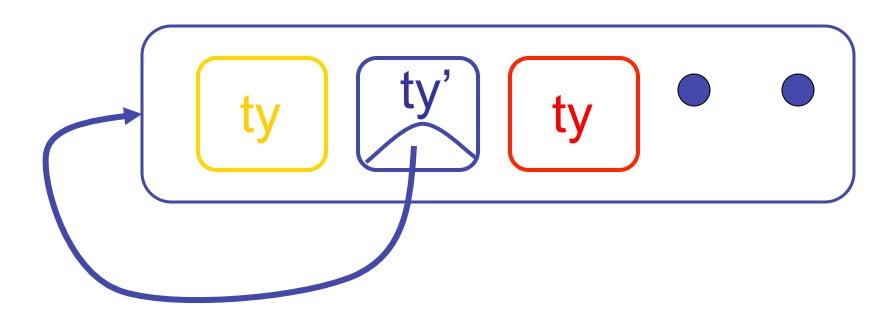
Folding over Variants

let optionFold someFun noneVal opt =
 match opt with None -> noneVal
 | Some x -> someFun x;;
val optionFold : ('a -> 'b) -> 'b -> 'a option ->
 'b = <fun>
let optionMap f opt =
 optionFold (fun x -> Some (f x)) None opt;;
val optionMap : ('a -> 'b) -> 'a option -> 'b

option = < fun >



The type being defined may be a component of itself



Recursive Data Types

type int_Bin_Tree =

Leaf of int | Node of (int_Bin_Tree *
 int_Bin_Tree);;

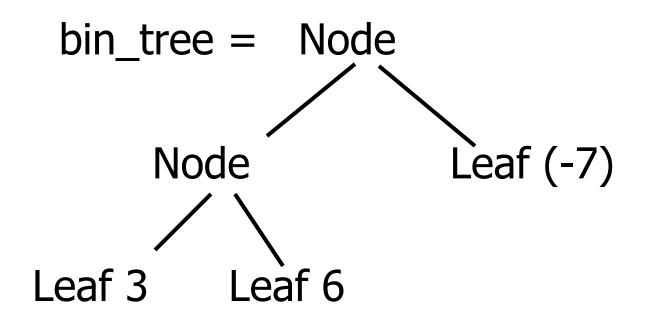
type int_Bin_Tree = Leaf of int | Node of (int_Bin_Tree * int_Bin_Tree)

Recursive Data Type Values

let bin_tree = Node(Node(Leaf 3, Leaf 6),Leaf (-7));;

val bin_tree : int_Bin_Tree = Node (Node (Leaf 3, Leaf 6), Leaf (-7))





Recursive Functions

let rec first_leaf_value tree =
 match tree with (Leaf n) -> n
 | Node (left_tree, right_tree) ->
 first_leaf_value left_tree;;
val first_leaf_value : int_Bin_Tree -> int =
 <fun>

let left = first_leaf_value bin_tree;;
val left : int = 3

Mapping over Recursive Types

let rec ibtreeMap f tree = match tree with (Leaf n) \rightarrow Leaf (f n) Node (left_tree, right_tree) -> Node (ibtreeMap f left_tree, ibtreeMap f right tree);; val ibtreeMap : (int -> int) -> int_Bin_Tree -> int Bin Tree = <fun>

Mapping over Recursive Types

ibtreeMap ((+) 2) bin_tree;;

- : int_Bin_Tree = Node (Node (Leaf 5, Leaf 8), Leaf (-5))

Folding over Recursive Types

let rec ibtreeFoldRight leafFun nodeFun tree = match tree with Leaf $n \rightarrow \text{leafFun} n$ | Node (left_tree, right_tree) -> nodeFun (ibtreeFoldRight leafFun nodeFun left tree) (ibtreeFoldRight leafFun nodeFun right tree);; val ibtreeFoldRight : (int -> 'a) -> ('a -> 'a -> 'a) ->int Bin Tree -> 'a = <fun>

Folding over Recursive Types

let tree_sum =

ibtreeFoldRight (fun x -> x) (+);;

val tree_sum : int_Bin_Tree -> int = <fun>

- # tree_sum bin_tree;;
- : int = 2

Mutually Recursive Types

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a

tree * 'a treeList)

Mutually Recursive Types - Values

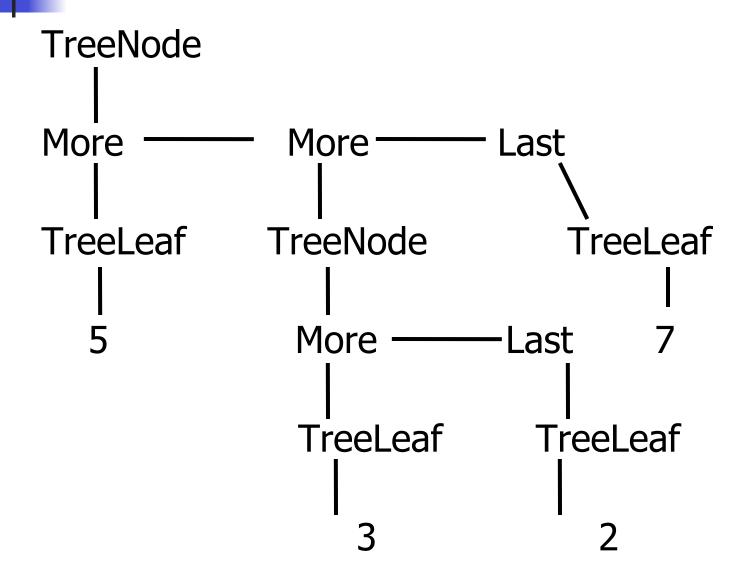
let tree =

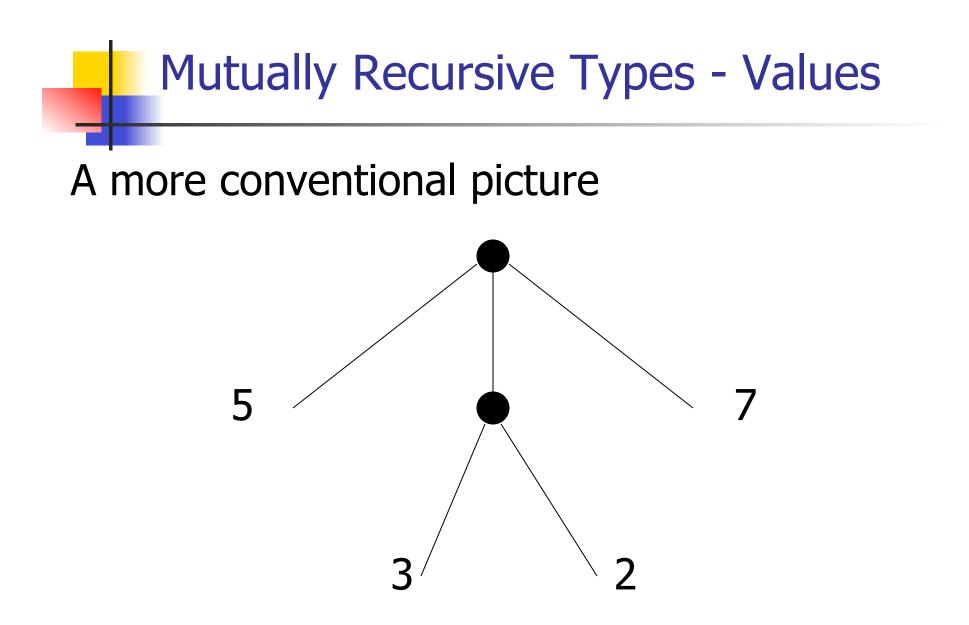
TreeNode (More (TreeLeaf 5, (More (TreeNode (More (TreeLeaf 3, Last (TreeLeaf 2))), Last (TreeLeaf 7)))));;

Mutually Recursive Types - Values

val tree : int tree =
 TreeNode
 (More
 (TreeLeaf 5,
 More
 (TreeNode (More (TreeLeaf 3, Last
 (TreeLeaf 2))), Last (TreeLeaf 7))))

Mutually Recursive Types - Values





Mutually Recursive Functions

let rec fringe tree =
 match tree with (TreeLeaf x) -> [x]
 (TreeNode list) -> list_fringe list
and list_fringe tree_list =
 match tree_list with (Last tree) -> fringe tree
 (More (tree,list)) ->
 (fringe tree) @ (list_fringe list);;

val fringe : 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>

Mutually Recursive Functions

fringe tree;;

- : int list = [5; 3; 2; 7]

Nested Recursive Types

type 'a labeled_tree = TreeNode of ('a * 'a labeled_tree list);; type 'a labeled_tree = TreeNode of ('a * 'a labeled_tree list)

Nested Recursive Type Values

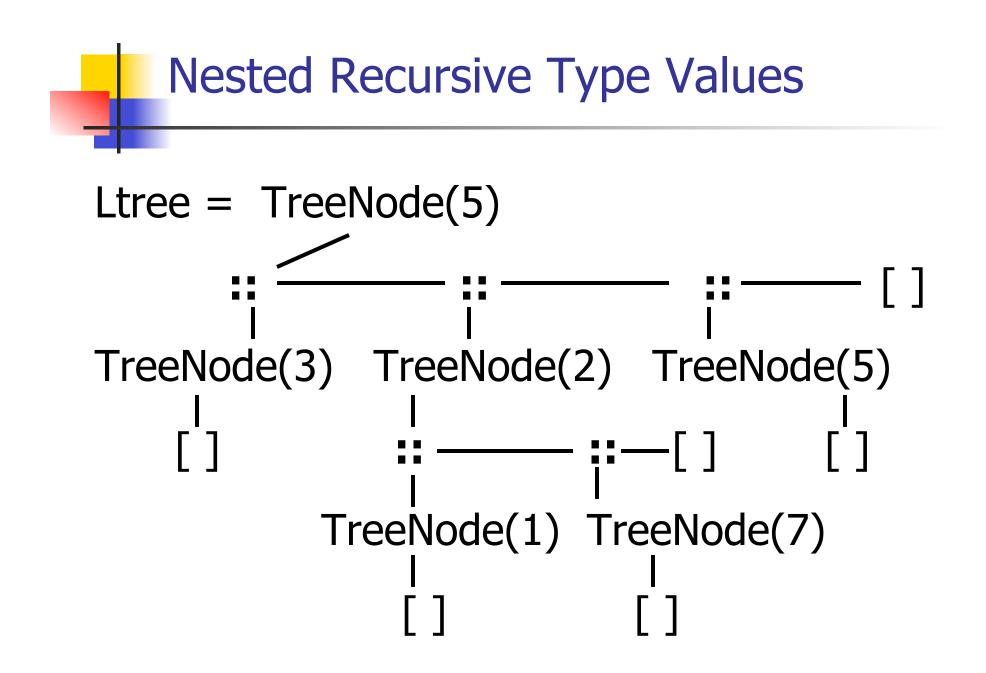
let ltree =

TreeNode(5, [TreeNode (3, []); TreeNode (2, [TreeNode (1, []); TreeNode (7, [])]); TreeNode (5, [])]);; **Nested Recursive Type Values**

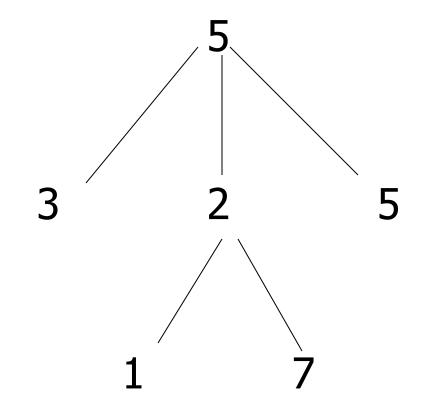
val ltree : int labeled_tree =

TreeNode

(5, [TreeNode (3, []); TreeNode (2, [TreeNode (1, []); TreeNode (7, [])]); TreeNode (5, [])])



Nested Recursive Type Values



Mutually Recursive Functions

let rec flatten_tree labtree = match labtree with TreeNode (x,treelist) -> x::flatten tree list treelist and flatten tree list treelist = match treelist with [] -> []labtree::labtrees -> flatten tree labtree @ flatten tree list labtrees;;

Mutually Recursive Functions

val flatten_tree : 'a labeled_tree -> 'a list = <fun>

val flatten_tree_list : 'a labeled_tree list -> 'a list = <fun>

- # flatten_tree ltree;;
- : int list = [5; 3; 2; 1; 7; 5]

Nested recursive types lead to mutually recursive functions

```
\# let rec ones = 1::ones;;
val ones : int list =
 [1; 1; 1; 1; ...]
# match ones with x::_ -> x;;
Characters 0-25:
Warning: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
 match ones with x:: -> x;;
```

```
^^^^
```

```
-: int = 1
```

let rec lab_tree = TreeNode(2, tree_list) and tree_list = [lab_tree; lab_tree];;

val lab tree : int labeled tree = TreeNode (2, [TreeNode(...); TreeNode(...)]) val tree list : int labeled tree list = [TreeNode (2, [TreeNode(...); TreeNode (...)]); TreeNode (2, [TreeNode(...); TreeNode (...)])]

match lab_tree with TreeNode (x, _) -> x;;

-: int = 2

Records

- Records serve the same programming purpose as tuples
- Provide better documentation, more readable code
- Allow components to be accessed by label instead of position
 - Labels (aka *field names* must be unique)
 - Fields accessed by suffix dot notation

Record Types

 Record types must be declared before they can be used in OCaml

type person = {name : string; ss : (int * int * int); age : int};;

type person = { name : string; ss : int * int *
int; age : int; }

person is the type being introduced

name, ss and age are the labels, or fields

Record Values

- Records built with labels; order does not matter
- # let teacher = {name = "Elsa L. Gunter"; age = 102; ss = (119,73,6244)};;
- val teacher : person =
 {name = "Elsa L. Gunter"; ss = (119, 73,
 6244); age = 102}

Record Values

- # let student = {ss=(325,40,1276); name="Joseph Martins"; age=22};; val student : person = {name = "Joseph Martins"; ss = (325, 40, 1276); age = 22} # student = teacher;;
- -: bool = false

Record Pattern Matching

let {name = elsa; age = age; ss = (_,_,s3)} = teacher;;

- val elsa : string = "Elsa L. Gunter"
- val age : int = 102
- val s3 : int = 6244



let soc_sec = teacher.ss;; val soc_sec : int * int * int = (119, 73, 6244)

New Records from Old

- # let birthday person = {person with age =
 person.age + 1};;
- val birthday : person -> person = <fun>
- # birthday teacher;;
- : person = {name = "Elsa L. Gunter"; ss = (119, 73, 6244); age = 103}

New Records from Old

let new_id name soc_sec person =

{person with name = name; ss = soc_sec};;
val new_id : string -> int * int * int -> person
 -> person = <fun>

- # new_id "Guieseppe Martin" (523,04,6712)
 student;;
- : person = {name = "Guieseppe Martin"; ss = (523, 4, 6712); age = 22}