## Programming Languages and Compilers (CS 421)

## Elsa L Gunter <br> 2112 SC, UIUC http://www.cs.illinois.edu/class/cs421/

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

## Contact Information - Elsa L Gunter

- Office: 2112 SC
- Office hours:
- Tuesdays 12:30pm - 1:45pm
- Wednesday 11:00am - 11:50am
- Thursdays 3:30pm - 4:15pm
- Also by appointment
- Email: egunter@illinois.edu


## Contact Information - TAs

- Teaching Assistants Office: 0207 SC
- Dennis Griffith
- Email: dgriffi3@illinois.edu
- Hours: Tues 5:00pm - 5:50pm \& Wed 12:30pm - 1:20pm
- Choonghwan Lee
- Email: clee83@illinois.edu
- Hours: Mon 9:00am - 9:50am \& Fri 1:00pm 1:50pm


## Course Website

- Main page - summary of news items
- Policy - rules governing course
- Lectures - syllabus and slides
- MPs - information about homework
- Exams
- Unit Projects - for 4 credit students
- Resources - tools and helpful info
- FAQ


## Some Course References

- No required textbook.
- Essentials of Programming Languages (2nd Edition) by Daniel P. Friedman, Mitchell Wand and Christopher T. Haynes, MIT Press 2001.
- Compilers: Principles, Techniques, and Tools, (also known as "The Dragon Book"); by Aho, Sethi, and Ullman. Published by Addison-Wesley. ISBN: 0-201-10088-6.
- Modern Compiler Implementation in ML by Andrew W. Appel, Cambridge University Press 1998
- Additional ones for Ocaml given separately


## Course Grading

- Homework 20\%
- About 9 MPs (in Ocaml) and 3 written assignments
- MPs submitted by handin on EWS linux machines
- HWs turned in in class
- Late submission penalty: 20\% of assignments total value
- 2 Midterms - 20\% each
- In class - Oct 11, Nov 10
- DO NOT MISS EXAM DATES!
- Final $40 \%$ - Dec 16, 7:00pm - 10:00pm
- Percentages are approximate
- Exams may weigh more if homework is much better


## Course Homework

- You may discuss homeworks and their solutions with others
- You may work in groups, but you must list members with whom you worked if you share solutions or solution outlines
- Each student must turn in their own solution separately
- You may look at examples from class and other similar examples from any source
- Note: University policy on plagiarism still holds - cite your sources if you are not the sole author of your solution
- Problems from homework may appear verbatim, or with some modification on exams


## Course Objectives

- New programming paradigm
- Functional programming
- Tail Recursion
- Continuation Passing Style
- Phases of an interpreter / compiler
- Lexing and parsing
- Type checking
- Evaluation
- Programming Language Semantics
- Lambda Calculus
- Operational Semantics


## OCAML

- Compiler is on the EWS-linux systems at
- /usr/local/bin/ocaml
- A (possibly better, non-PowerPoint) text version of this lecture can be found at
- http://www.cs.illinois.edu/class/cs421/ lectures/ocaml-intro-shell.txt
- For the OCAML code for today's lecture see
- http://www.cs.illinois.edu/class/cs421/ lectures/ocaml-intro.ml


## WWW Addresses for OCAML

- Main CAML home: http://caml.inria.fr/index.en.html
- To install OCAML on your computer see:
-_ http://caml.inria.fr/ocaml/release.en.html


## References for CAML

- Supplemental texts (not required):
- The Objective Caml system release 3.09, by Xavier Leroy, online manual
- Introduction to the Objective Caml Programming Language, by Jason Hickey
- Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O'Reilly
- Available online from course resources


## OCAML

- CAML is European descendant of original ML
- American/British version is SML
- O is for object-oriented extension
- ML stands for Meta-Language
- ML family designed for implementing theorem provers
- It was the meta-language for programming the "object" language of the theorem prover
- Despite obscure original application area, OCAML is a full general-purpose programming language


## Features of OCAML

- Higher order applicative language
- Call-by-value parameter passing
- Modern syntax
- Parametric polymorphism
- Aka structural polymorphism
- Automatic garbage collection
- User-defined algebraic data types
- It's fast - winners of the 1999 and 2000 ICFP Programming Contests used OCAML


## Why learn OCAML?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCAML is particularly efficient for programming tasks involving languages (eg parsing, compilers, user interfaces)
- Used at Microsoft for writing SLAM, a formal methods tool for C programs


## Session in OCAML

\% ocaml
Objective Caml version 3.12.0
\# (* Read-eval-print loop; expressions and declarations
$2+3 ;$ (* Expression *)

- : int $=5$
\#
\# 3 < 2; ;
- : bool = false


## No Overloading for Basic Arithmetic Operations

\# 15 * 2; ;

- : int = 30
\# 1.35 + 0.23;; (* Wrong type of addition *)
Characters 0-4:
$1.35+0.23 ;$ (* Wrong type of addition *) ^^^^

Error: This expression has type float but an expression was expected of type int
\# 1.35 +. 0.23;;

- : float = 1.58


## No Implicit Coercion

\# 1.0 * 2;; (* No Implicit Coercion *)
Characters 0-3:
1.0 * 2;; (* No Implicit Coercion *)

ヘヘ^
Error: This expression has type float but an expression was expected of type int

## Sequencing Expressions

## \# "Hi there";; (* has type string *)

- : string = "Hi there"
\# print_string "Hello world \n";; (* has type unit *)
Hello world
- : unit = ()
\# (print_string "Bye\n"; 25);; (* Sequence of exp *)
Bye
- : int = 25


## Terminology

- Output refers both to the result returned from a function application
- As in + outputs integers, whereas +. outputs floats
- And to text printed as a side-effect of a computation
- As in print_string " $\backslash n$ " outputs a carriage return
- In terms of values, it outputs ( ) ("unit")
- We will standardly use "output" to refer to the value returned


## Declarations; Sequencing of Declarations

\# let $\mathrm{x}=2+3 ;$ (* declaration *)
val $x$ : int $=5$
\# let test = $3<2$;
val test : bool = false
\# let $\mathrm{a}=3$ let $\mathrm{b}=\mathrm{a}+2 ;$; (* Sequence of dec *)
val a : int = 3
val b:int=5

## Environments

- Environments record what value is associated with a given variable
- Central to the semantics and implementation of a language
- Notation

$$
\rho=\left\{\text { name }_{1} \rightarrow \text { value }_{1}, \text { name }_{2} \rightarrow \text { value }_{2}, \ldots\right\}
$$

Using set notation, but describes a partial function

- Often stored as list, or stack
- To find value start from left and take first match


## Global Variable Creation

\# 2 + 3; ; (* Expression *)
// doesn't effect the environment
\# let test $=3<2 ; \% \quad(*$ Declaration *)
val test : bool = false
// $\rho=\{$ test $\rightarrow$ false $\}$
\# let $\mathrm{a}=3$ let $\mathrm{b}=\mathrm{a}+2 ;$; (* Sequence of dec *)
// $\rho=\{b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$

## Local let binding

\# let b = 5 * 4 in 2 * b;;

- : int = 40
// $\rho=\{b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# let c =
let $\mathrm{b}=\mathrm{a}+\mathrm{a}$
in $b$ * b;;
val c : int $=36$
// $\rho=\{c \rightarrow 36, b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# b;;
- : int = 5


## Local Variable Creation

\# let c =
let $\mathrm{b}=\mathrm{a}+\mathrm{a}$
$/ / \rho 1=\{b \rightarrow 6, a \rightarrow 3$, test $\rightarrow$ false $\}$
in b * b ;;
val c: int $=36$
$/ / \rho=\{c \rightarrow 36, b \rightarrow 5, a \rightarrow 3$, test $\rightarrow$ false $\}$
\# b;;

- : int = 5


## Booleans (aka Truth Values)

\# true;,

- : bool = true
\# false;,"
- : bool = false

$$
\begin{aligned}
& \text { \# if } y>x \text { then } 25 \text { else 0; } \\
& \text { - : int }=25
\end{aligned}
$$

## Booleans

\# 3 > 1 \&\& 4 > 6;;

- : bool = false
\# 3 > 1 || 4 > 6;;
- : bool = true
\# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
Hi
- : bool = true
\# 3 > 1 || (print_string "Bye\n"; 4 > 6);;
- : bool = true
\# not (4 > 6);;
- : bool = true


## Tuples

\# let s = (5,"hi",3.2);;
val s : int * string * float $=(5$, "hi", 3.2)
\# let $(\mathrm{a}, \mathrm{b}, \mathrm{c})=\mathrm{s} ;$; ( $\quad(\mathrm{a}, \mathrm{b}, \mathrm{c})$ is a pattern *)
val a : int = 5
val b : string = "hi"
val c: float $=3.2$
\# let $x=2,9.3 ;$; (* tuples don't require parens in Ocaml *)
val $x$ : int * float $=(2,9.3)$

## Tuples

\# (*Tuples can be nested *)
let d = ((1,4,62),("bye",15),73.95);;
val d : (int * int * int) * (string * int) * float $=$
((1, 4, 62), ("bye", 15), 73.95)
\# (*Patterns can be nested *)
let $\left(p,\left(s t, \_\right),{ }_{\prime}\right)=d_{;} ;$(* $^{*}$ matches all, binds nothing *)
val p : int * int * int $=(1,4,62)$
val st : string = "bye"

## Functions

\# let plus_two $\mathrm{n}=\mathrm{n}+2$ 2;
val plus_two : int -> int = <fun>
\# plus_two 17, ;,

- : int = 19
\# let plus_two $=$ fun $\mathrm{n}->\mathrm{n}+2 ;$;
val plus_two : int -> int = <fun>
\# plus_two 14;,;
- : int = 16

First definition syntactic sugar for second

## Using a nameless function

\# (fun $x->x * 3) 5$; $;$ (* An application *)

- : int = 15
\# ((fun y -> y +. 2.0), (fun z -> z * 3)) ;" (* As data *)
- : (float -> float) $*$ (int $->$ int $)=(<$ fun $>$, <fun>)

Note: in fun $v->\exp (v)$, scope of variable is only the body $\exp (\mathrm{v})$

## Values fixed at declaration time

\# let x = 12;;
val x : int $=12$
\# let plus_x y = y + x ; ;
val plus_x : int -> int = <fun>
\# plus_x 3;;
What is the result?

## Values fixed at declaration time

\# let x = 12;;
val x : int $=12$
\# let plus_x y = y + x ; ;
val plus_x : int -> int = <fun>
\# plus_x 3;;

- : int = 15


## Values fixed at declaration time

\# let $x=7$; ; (* New declaration, not an update *)
val x : int = 7
\# plus_x 3;;

What is the result this time?

## Values fixed at declaration time

\# let $\mathrm{x}=7$; ; (* New declaration, not an update *)
val x : int = 7
\# plus_x 3;;

- : int = 15


## Functions on tuples

\# let plus_pair (n,m) = n + m; ;
val plus_pair : int * int -> int = <fun>
\# plus_pair (3,4);;

- : int = 7
\# let double $x=(x, x)$; ;
val double : 'a -> 'a * 'a = <fun>
\# double 3;;
- : int * int = $(3,3)$
\# double "hi";;
- : string * string = ("hi", "hi")


## Match Expressions

\# let triple_to_pair triple =

$$
\begin{aligned}
& \text { match triple } \\
& \text { with }(0, x, y)->(x, y) \\
& \mid(x, 0, y)->(x, y) \\
& \mid(x, y, \ldots)->(x, y) ; ;
\end{aligned}
$$

-Each clause: pattern on left, expression on right
-Each $x$, $y$ has scope of only its clause
-Use first matching clause
val triple_to_pair : int * int * int -> int * int = <fun>

## Functions with more than one argument

\# let add_three x y z = x + y + z; ;
val add_three : int $->$ int $->$ int $->$ int $=$ <fun>
\# let t = add_three 63 2;"
val t : int = 11

## Curried vs Uncurried

- Recall
val add_three : int -> int -> int -> int = <fun>
- How does it differ from
\# let add_triple ( $u, v, w)=u+v+w ; ;$
val add_triple : int * int * int -> int = <fun>
- add_three is curried;
- add_triple is uncurried


## Functions as arguments

\# let thrice $\mathrm{fx}=\mathrm{f}(\mathrm{f}(\mathrm{fx})$ ); ;
val thrice : ('a -> 'a) -> 'a -> 'a = <fun>
\# let g = thrice plus_two;;
val g : int -> int = <fun>
\# g 4;;

- : int = 10
\# thrice (fun s -> "Hi! " ^ s) "Good-bye!";;
- : string = "Hi! Hi! Hi! Good-bye!"


## Curried vs Uncurried

\＃add＿triple（6，3，2）；；
－：int＝ 11
\＃add＿triple 5 4；；
Characters 0－10：
add＿triple 5 4；；
ヘヘヘヘヘヘヘヘヘヘヘ
This function is applied to too many arguments， maybe you forgot a｀；＇
\＃fun x－＞add＿triple（ $5,4, \mathrm{x}$ ）；；
：int－＞int＝＜fun＞

## Partial application of functions

let add_three x y z = x + y + z; ;
\# let h = add_three 5 4;;
val h : int -> int = <fun>
\# h 3;;

- : int = 12
\# h 7;;
- : int = 16


## Question

- Observation: Functions are first-class values in this language
- Question: What value does the environment record for a function variable?
- Answer: a closure


## Save the Environment!

- A closure is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:

$$
\left.\mathrm{f} \rightarrow<(\mathrm{v} 1, \ldots, \mathrm{vn}) \rightarrow \exp , \rho_{\mathrm{f}}\right\rangle
$$

- Where $\rho_{f}$ is the environment in effect when $f$ is defined (if $f$ is a simple function)


## Closure for plus_x

- When plus_x was defined, had environment:

$$
\rho_{\text {plus_x }}=\{x \rightarrow 12, \ldots, y \rightarrow 24, \ldots\}
$$

- Closure for plus_x:

$$
\left\langle y \rightarrow y+x, \rho_{\text {plus_x }}>\right.
$$

- Environment just after plus_x defined:
$\left\{\right.$ plus_ $x \rightarrow\left\langle y \rightarrow y+x, \rho_{\text {plus_x }}>\right\}+\rho_{\text {plus_x }}$


## Closure for plus_pair

- Assume $\rho_{\text {plus_pair }}$ was the environment just before plus_pair defined
- Closure for plus_pair:

$$
<(\mathrm{n}, \mathrm{~m}) \rightarrow \mathrm{n}+\mathrm{m}, \rho_{\text {plus_pair }}>
$$

- Environment just after plus_pair defined:
$\left\{\right.$ plus_pair $\left.\rightarrow<(\mathrm{n}, \mathrm{m}) \rightarrow \mathrm{n}+\mathrm{m}, \rho_{\text {plus_pair }}>\right\}$ $+\rho_{\text {plus_pair }}$


## Evaluation of Application of plus_x;;

- Have environment:

$$
\begin{gathered}
\rho=\left\{\text { plus_x } x<y \rightarrow y+x, \rho_{\text {plus_x }}>, \ldots,\right. \\
y \rightarrow 3, \ldots\}
\end{gathered}
$$

where $\rho_{\text {plus_x }}=\{x \rightarrow 12, \ldots, y \rightarrow 24, \ldots\}$

- Eval (plus_x y, $\rho$ ) rewrites to
- Eval (app <y $\rightarrow y+x, \rho_{\text {plus_x }}>3, \rho$ ) rewrites to
- Eval ( $y+x,\{y \rightarrow 3\}+\rho_{\text {plus_x }}$ ) rewrites to
- $\operatorname{Eval}\left(3+12, \rho_{\text {plus_x }}\right)=15$


## Evaluation of Application with Closures

- In environment $\rho$, evaluate left term to closure, $c=\left\langle\left(x_{1}, \ldots, x_{n}\right) \rightarrow b, \rho\right\rangle$
- ( $\mathrm{x}_{1}, \ldots, \mathrm{x}_{\mathrm{n}}$ ) variables in (first) argument
- Evaluate the right term to values, $\left(\mathrm{v}_{1}, \ldots, \mathrm{v}_{\mathrm{n}}\right)$
- Update the environment $\rho$ to
$\rho^{\prime}=\left\{x_{1} \rightarrow v_{1}, \ldots, x_{n} \rightarrow v_{n}\right\}+\rho$
- Evaluate body b in environment $\rho^{\prime}$


## Scoping Question

Consider this code:
let $x=27 ;$
let $\mathrm{f} x=$
let $x=5$ in
(fun x -> print_int x) 10;;
f 12; ;
What value is printed?
5
10
12
27

## Recursive Functions

\# let rec factorial $\mathrm{n}=$
if $\mathrm{n}=0$ then 1 else n * factorial ( $\mathrm{n}-1$ );;
val factorial : int -> int = <fun>
\# factorial 5;;

- : int = 120
\# (* rec is needed for recursive function declarations *)
(* More on this later *)

