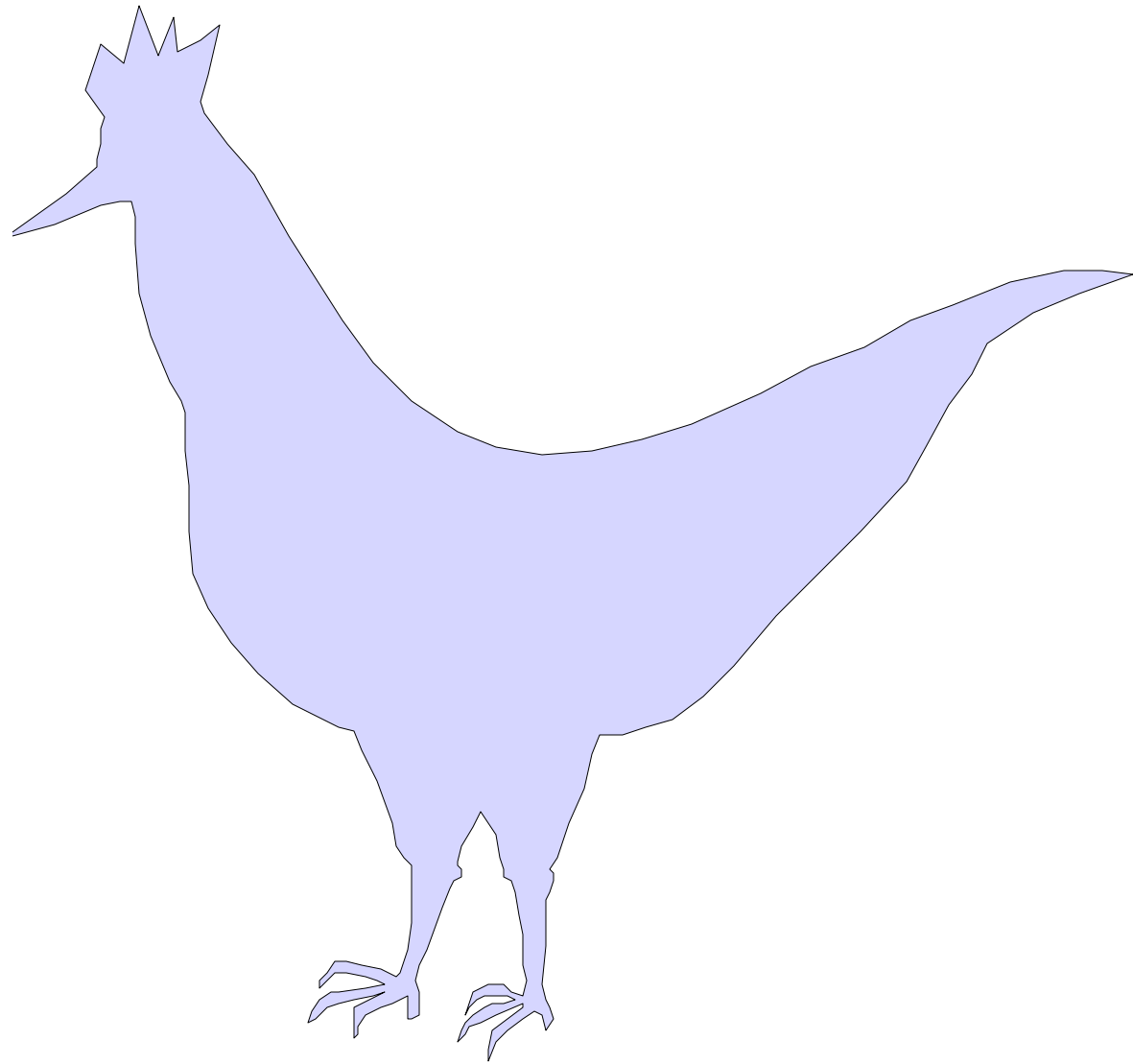


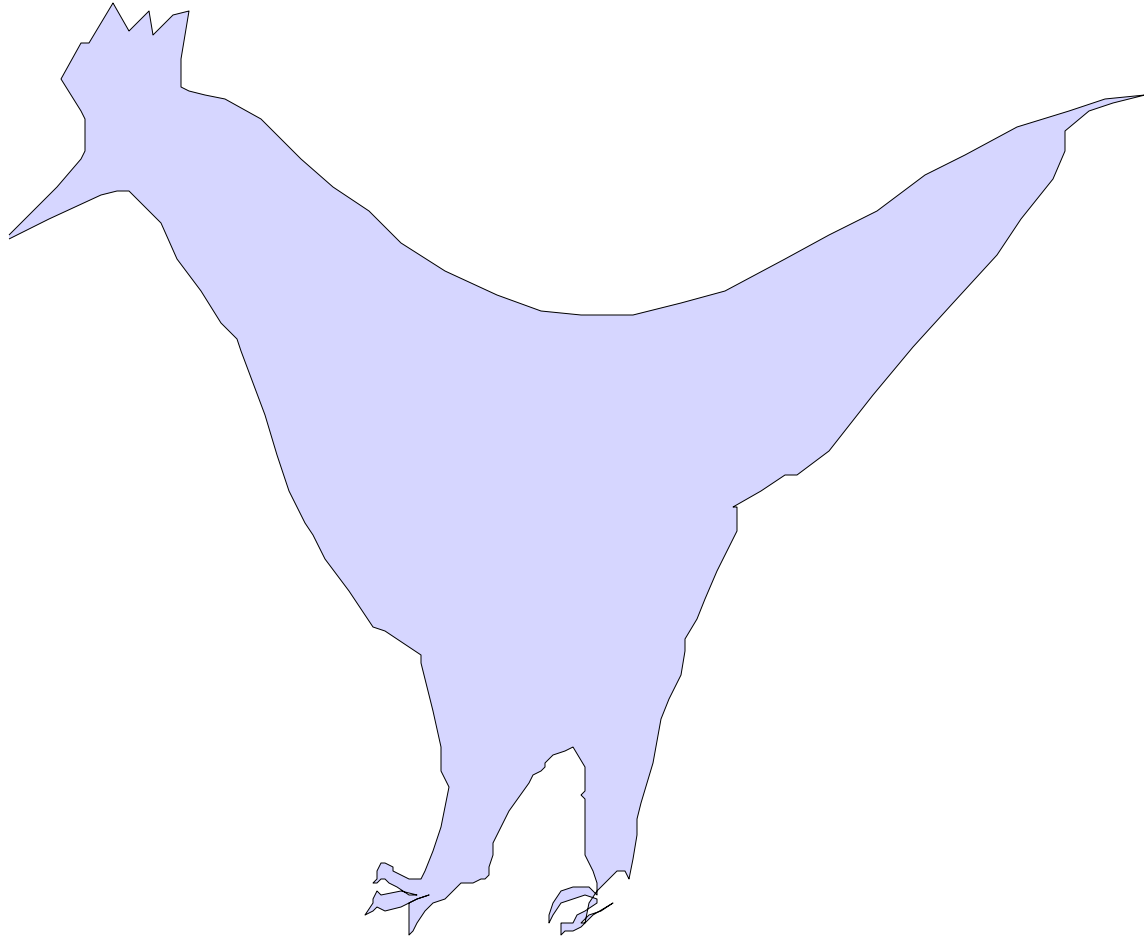
# Animation

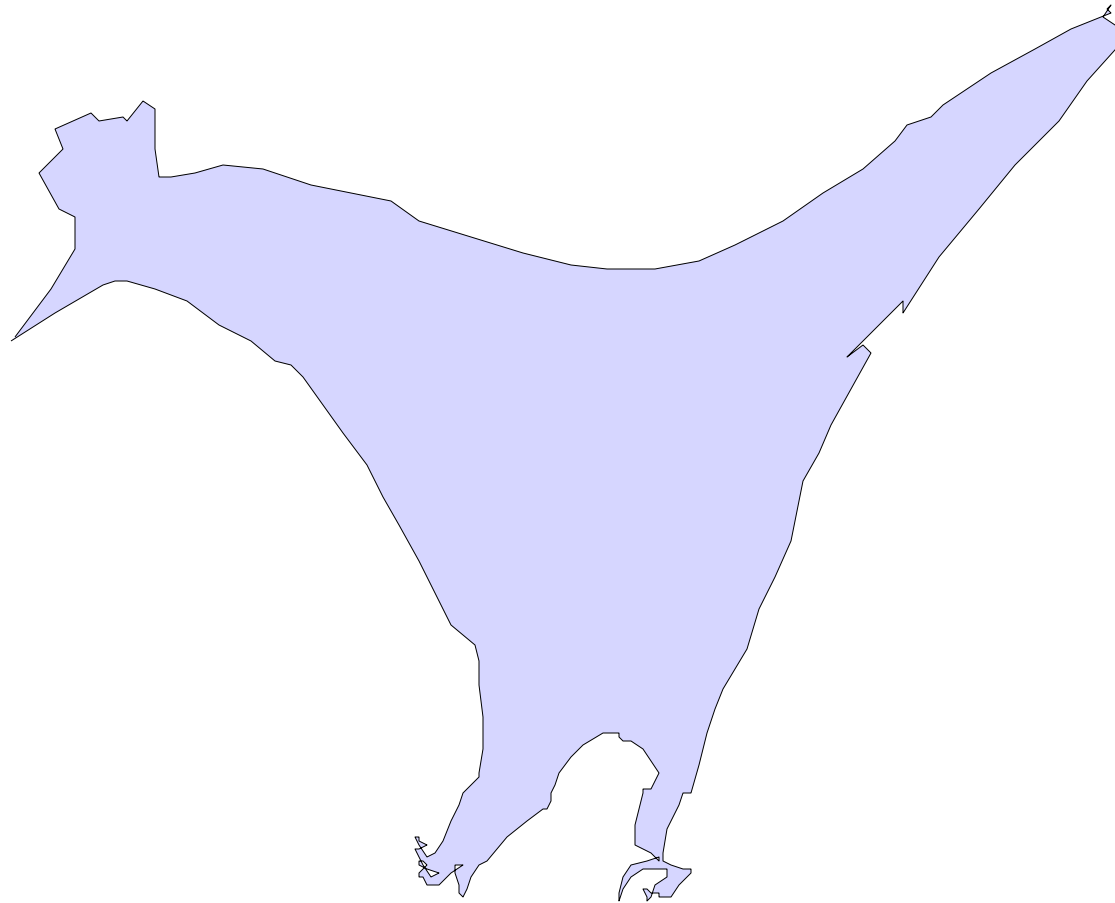
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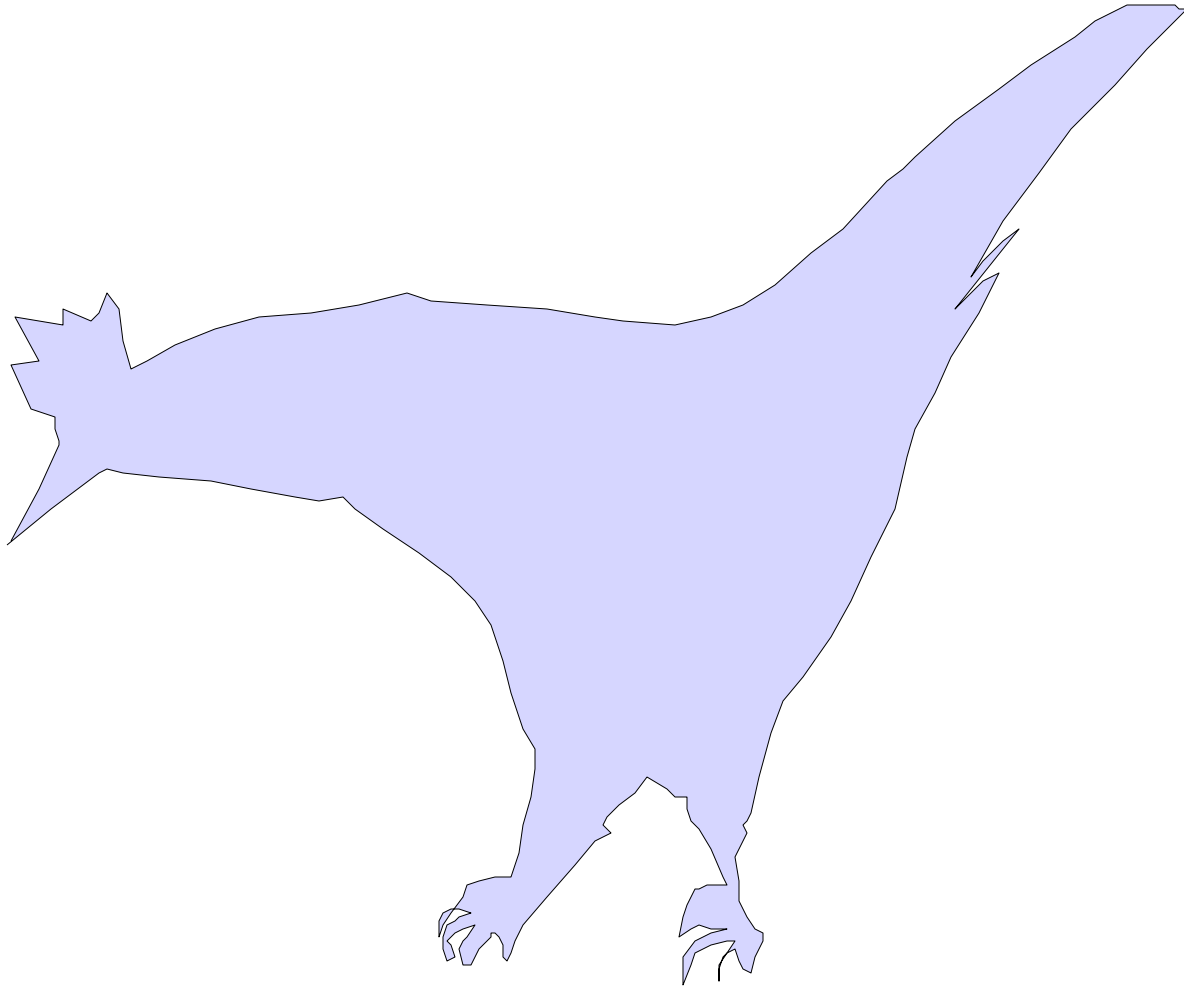
CS418 Computer Graphics

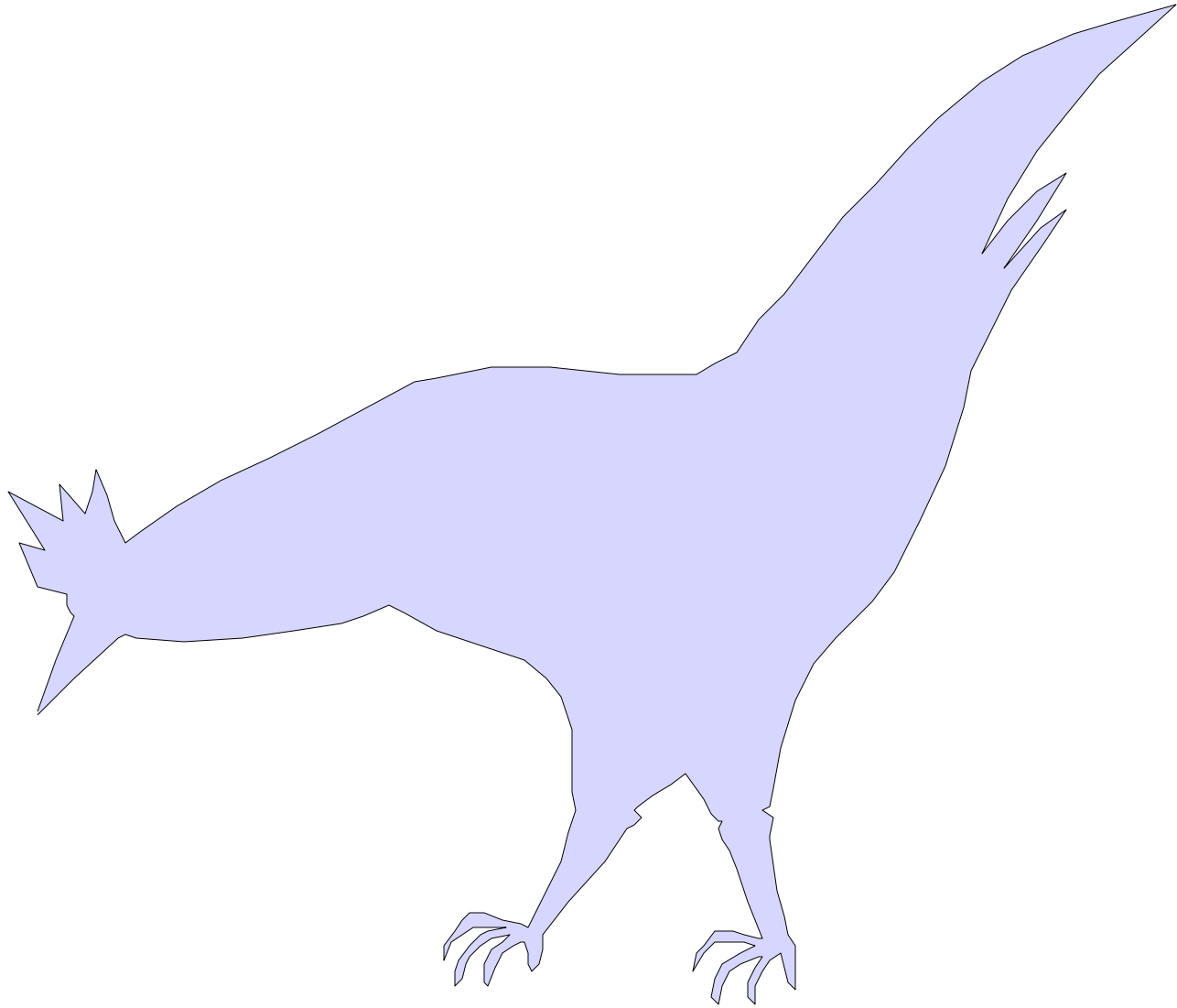
John C. Hart





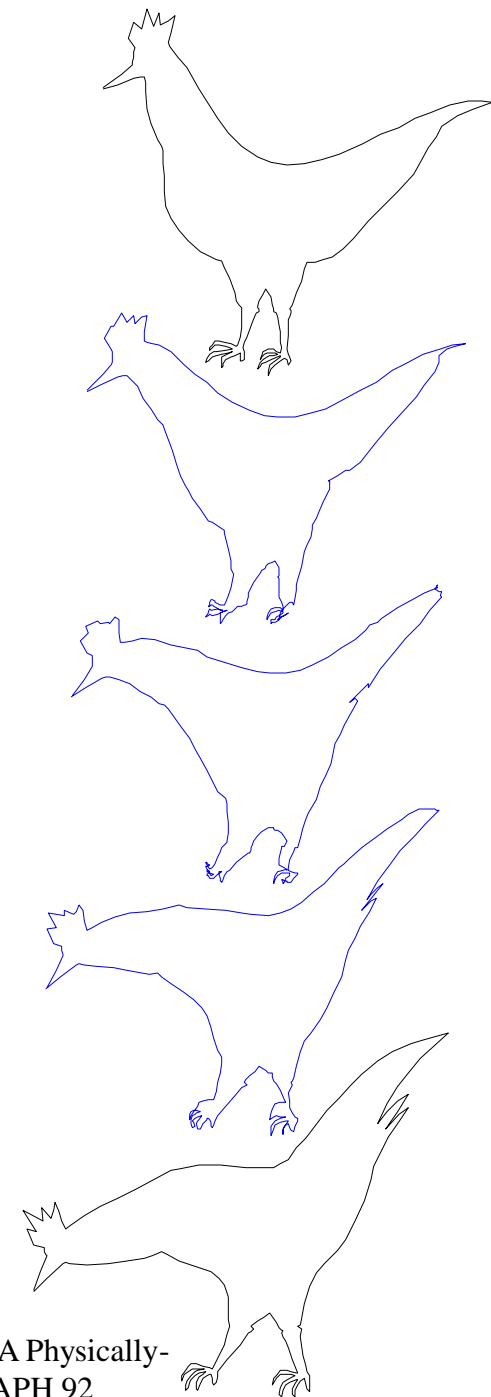






# Keyframe Animation

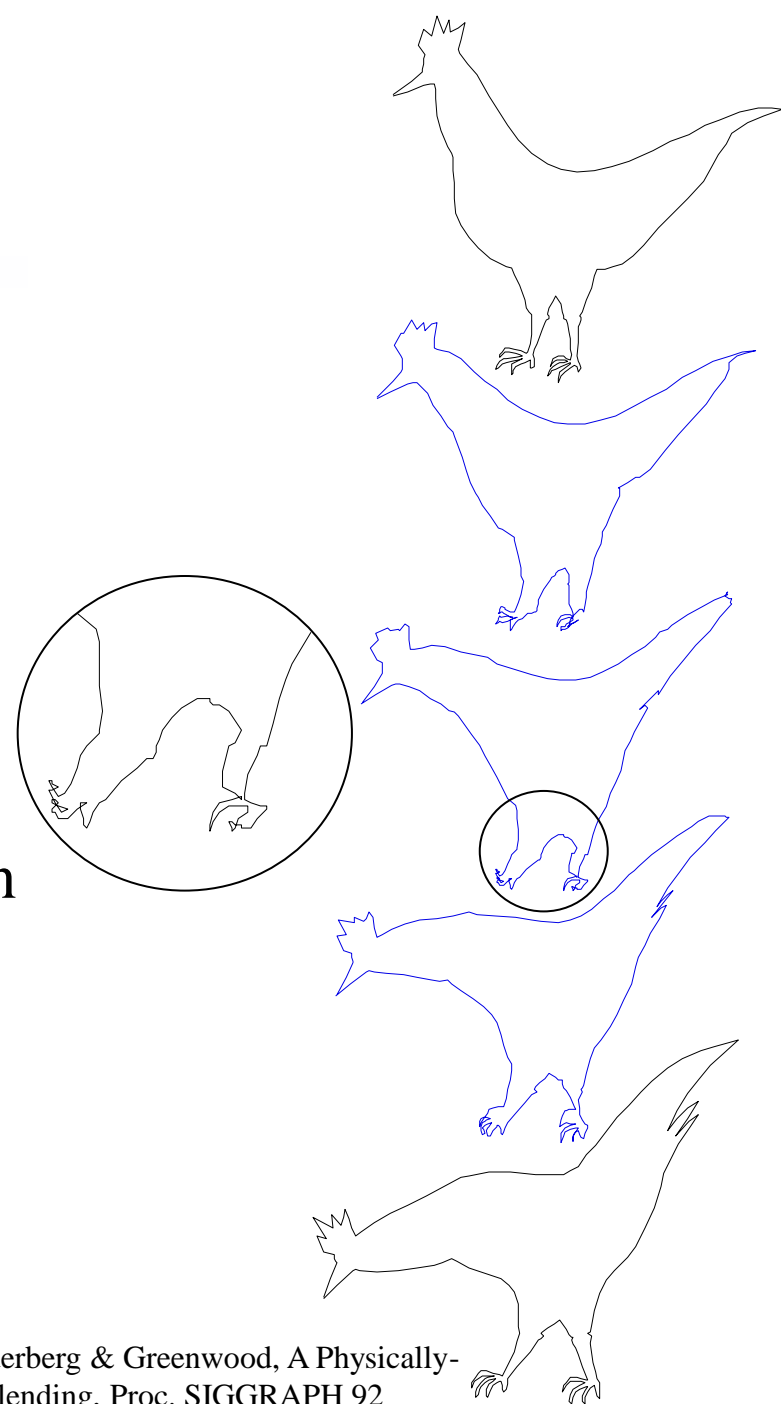
- Set target positions for vertices at “key” frames in animations
- Linearly interpolate vertex positions between targets at intervening frames
- Lots can go wrong (like the feet)
- Can be fixed by adding key frames
- Piecewise linear approach to animation
- Need same number and configuration of vertices at key frames for intervening frames to make sense
- Often need to find correspondences between two collections of vertices



A motivating example from: Sederberg & Greenwood, A Physically-Based Approach to 2-D Shape Blending, Proc. SIGGRAPH 92

# Keyframe Animation

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# Polar Decomposition

- Linear affine interpolation of transformation matrices does not accommodate rotation
- Let  $M$  be the upper-left 3x3 submatrix of a 4x4 homogeneous transformation matrix
- Decompose:  $M = QS$ 
  - $Q$ : non-linearly varying part (rotation)
  - $S$ : linearly varying part (scale, shear)
- Initialize  $Q = M$
- Replace  $Q = \frac{1}{2}(Q + Q^T)$  until it converges to a 3x3 rotation matrix ( $Q^T = Q^{-1}$ )
- Then  $Q$  contains the rotation part of  $M$
- And  $S = Q^T M$  contains the scaling part
- Interpolate  $S$  linearly per-element
- Interpolate  $Q$  using quaternions

