

# Buddy System and Segmentation

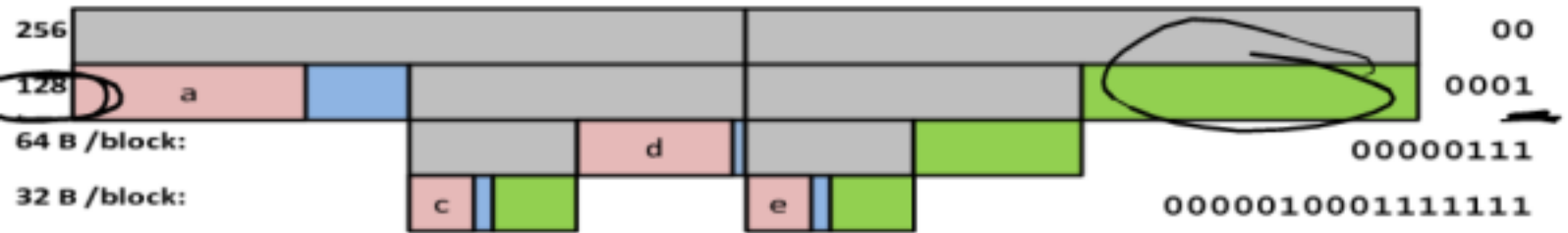
CS 241

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# More Buddy System

*malloc(100)*

- Last Lecture:

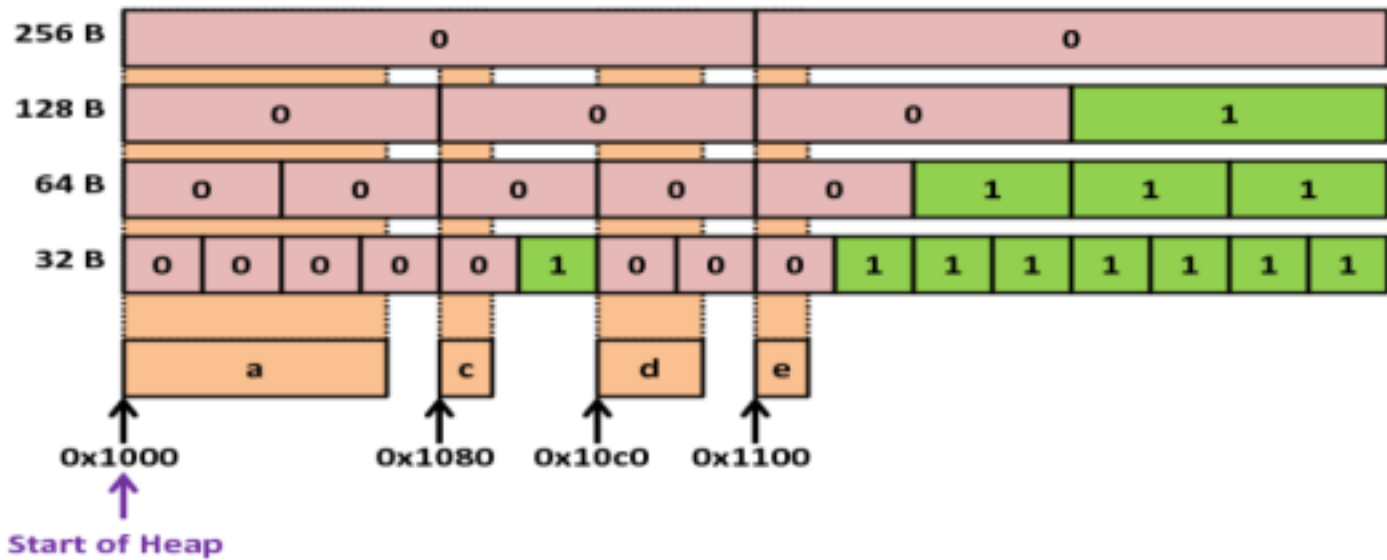


- Optimization:

- Multiple levels may each have their own bit masks.
  - **Advantage:** Speeds up finding open space
  - **Disadvantage:** Increased overhead

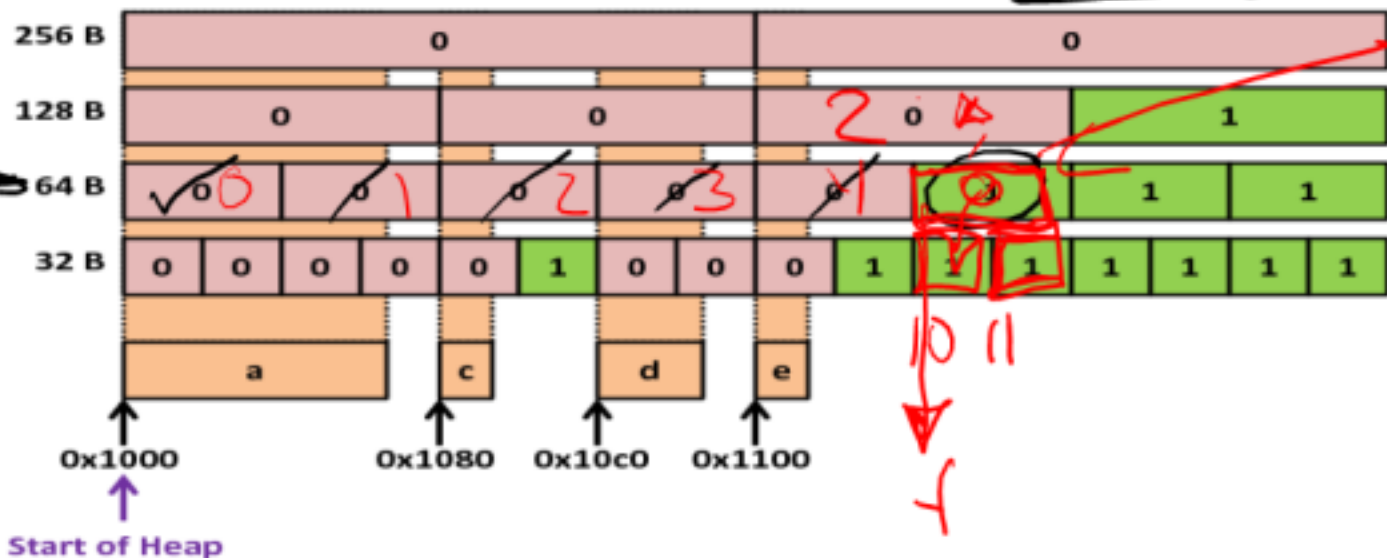
# Buddy System

- Represented as bitmaps:



# Buddy System <sup>64 = 0000000</sup>

• Request: `f = malloc(56) → 00111000`

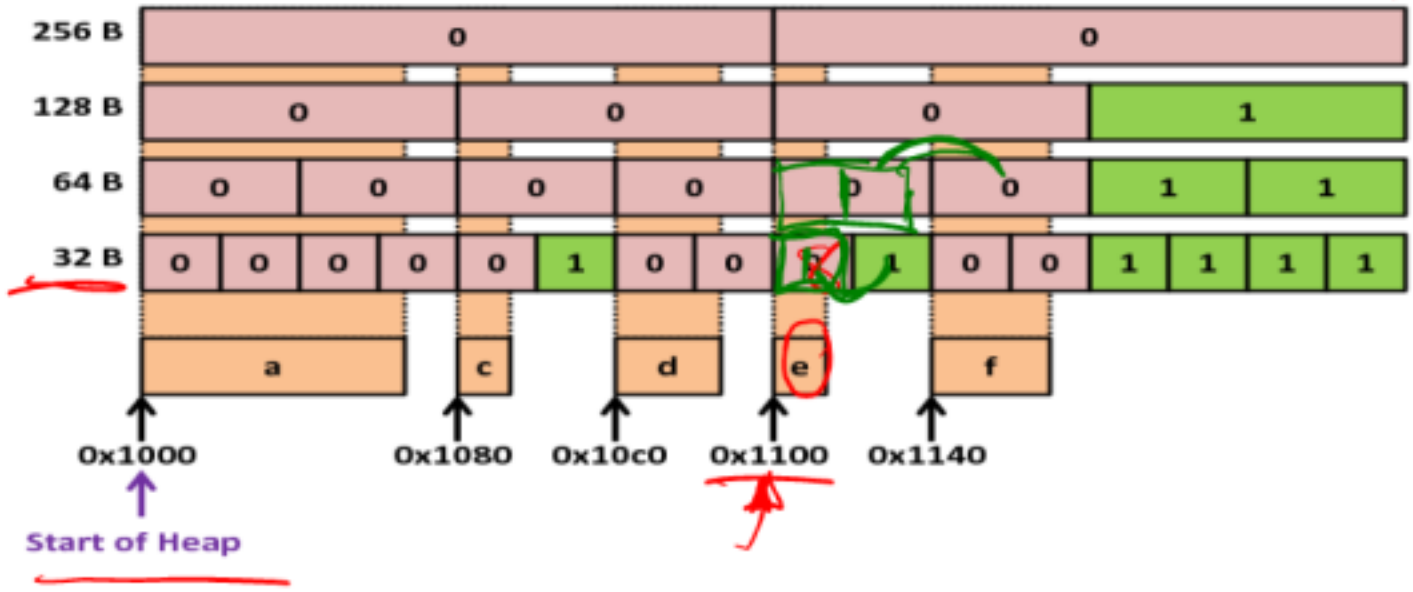


# Buddy System

$$\begin{array}{r} 1100 \\ - 1000 \\ \hline 0x1000 / 0x20 \end{array}$$

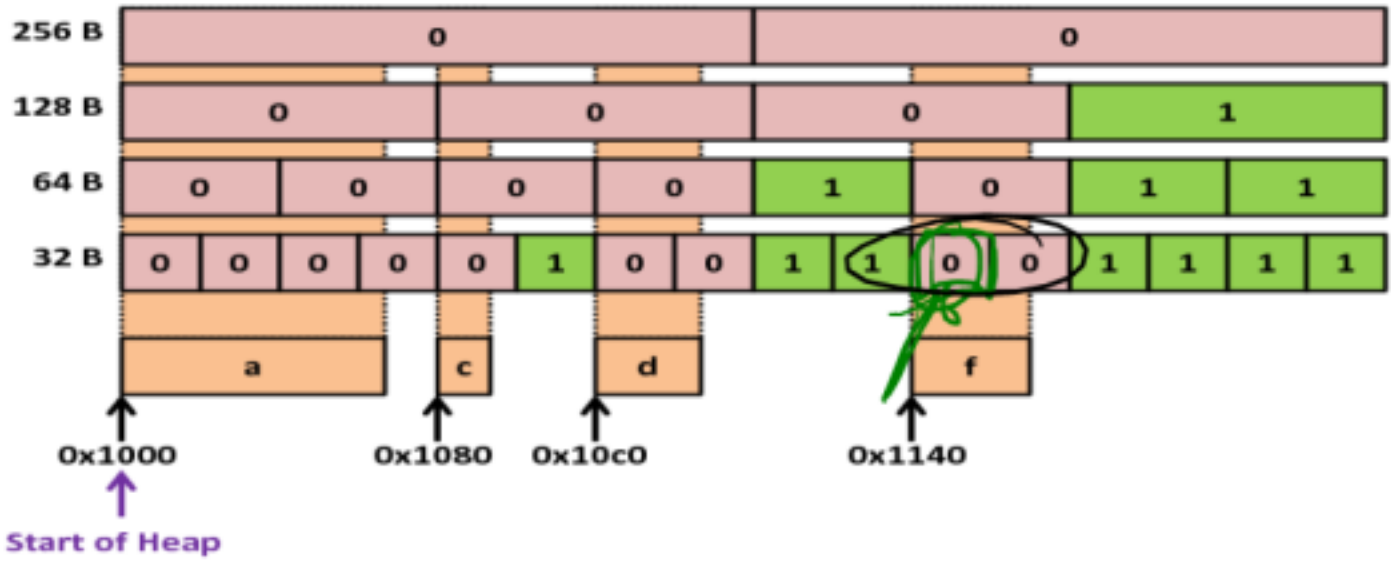
$8 =$

- Request: **free (e)**



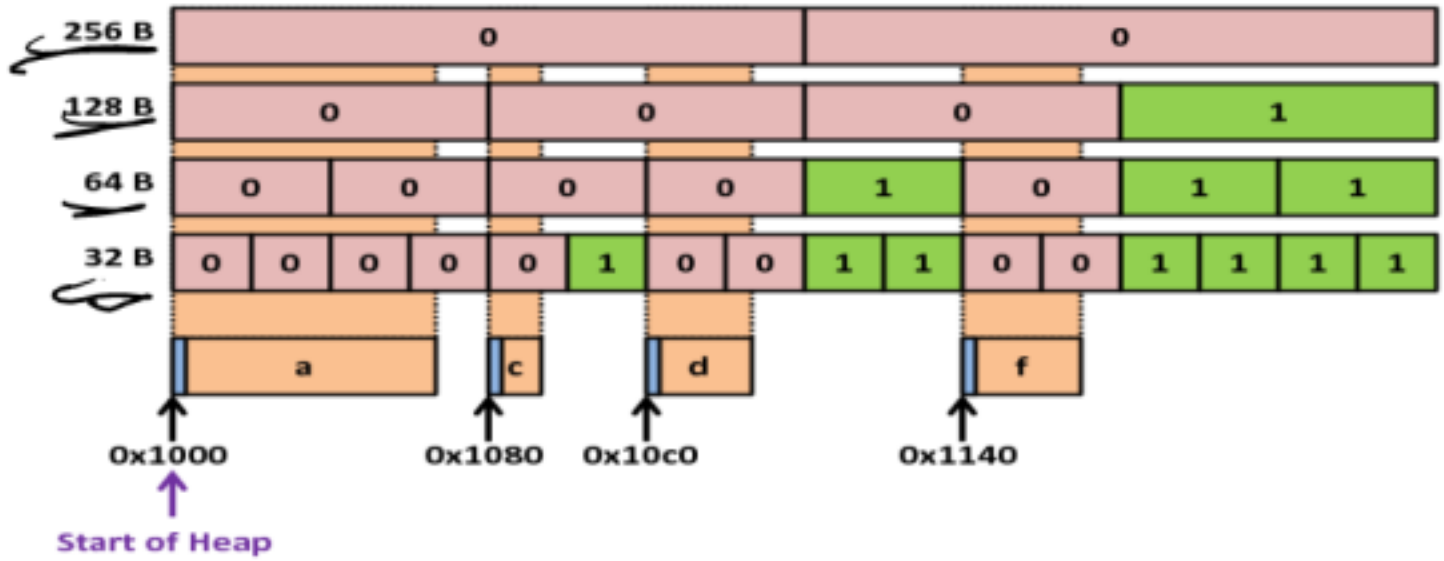
# Buddy System

- Request: **free (f)**



# Buddy System <sup>32</sup>

- Buddy System requires knowledge of level/size of allocation.



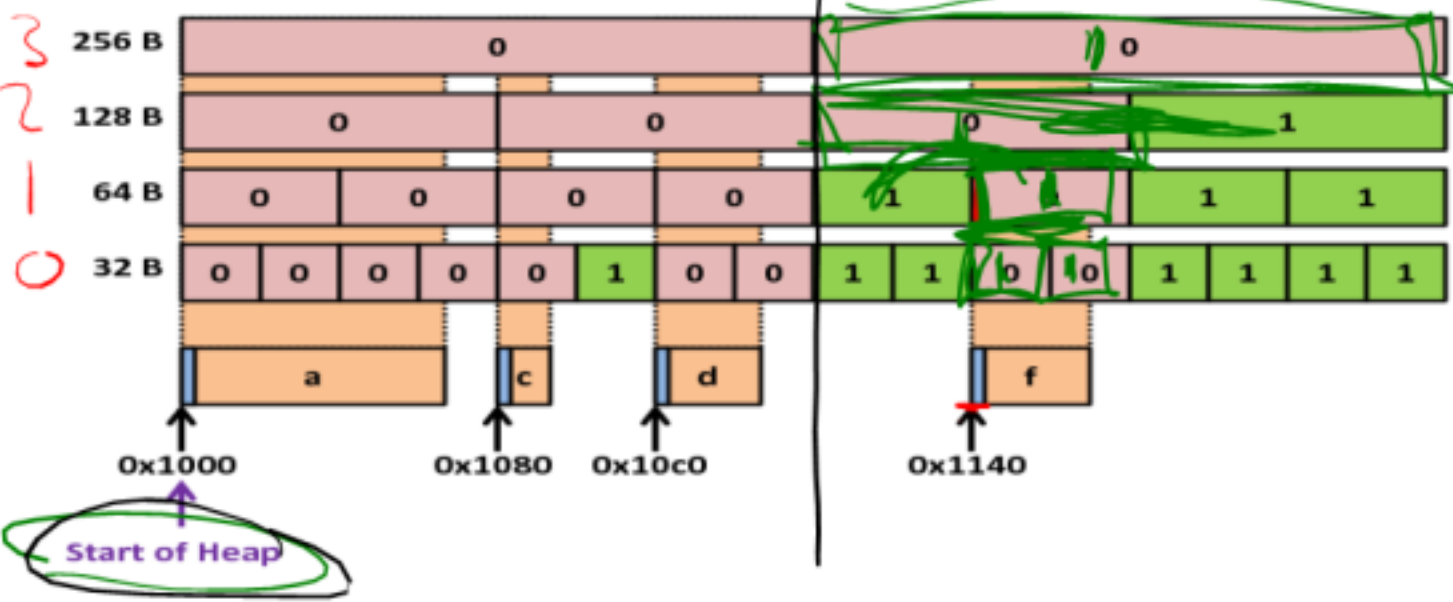
$$32 = 1000000$$

$$64 = 1000000$$




# Buddy System

- Request: **free (f)**

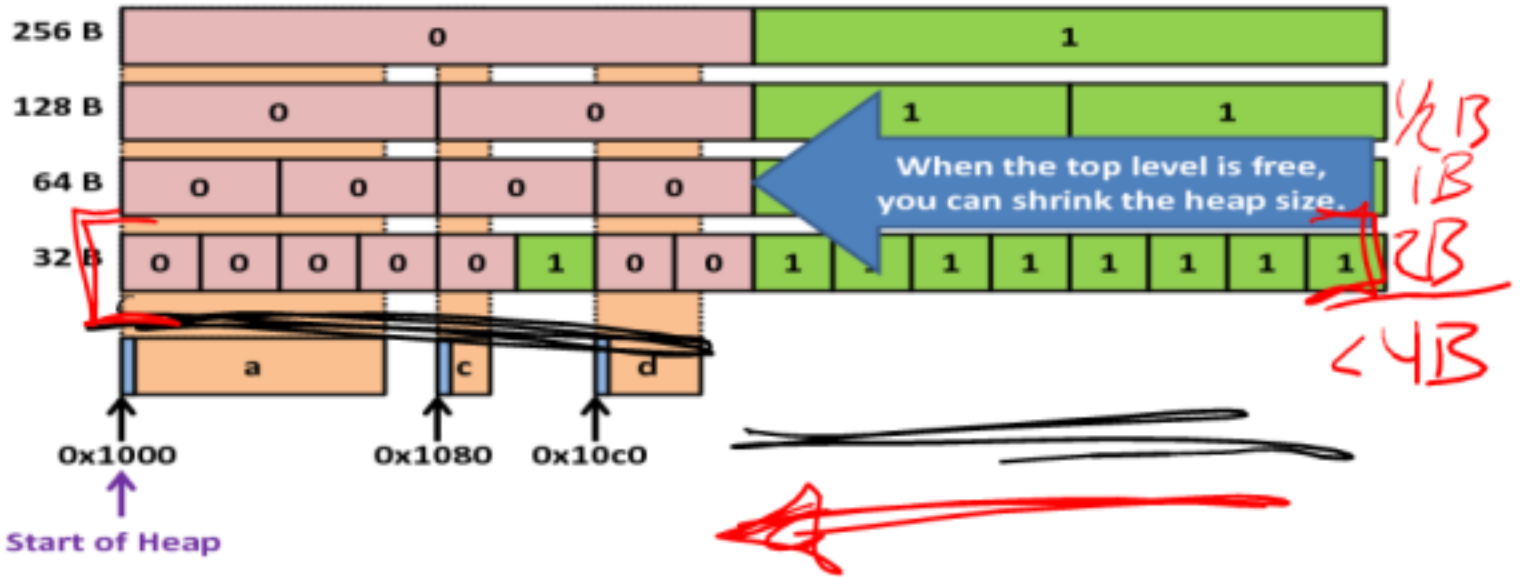


# Buddy System

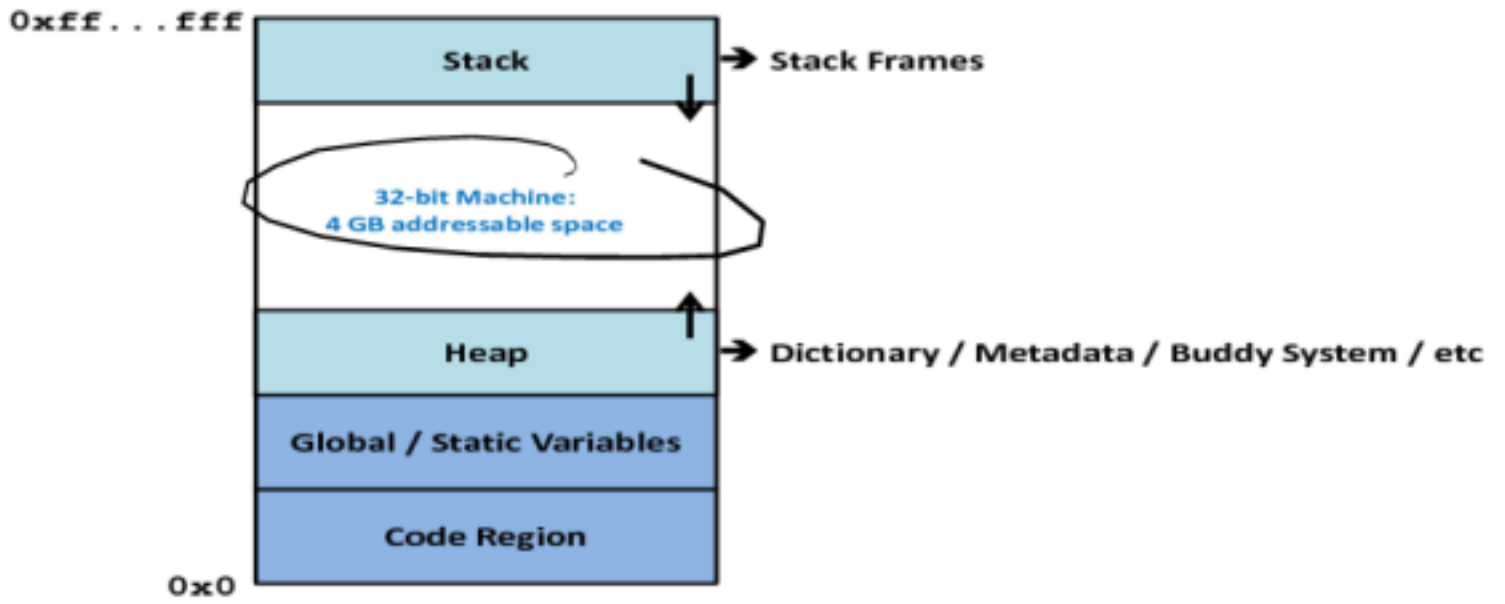
• Result:

*work()*

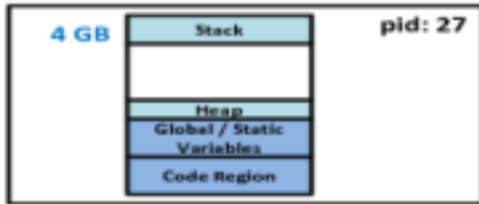
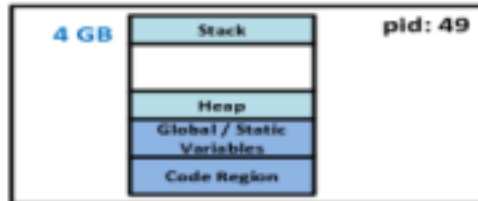
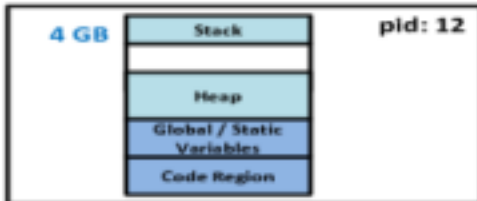
*work(0)*



# Up to now...



# Every process has their own virtual memory space..



# Virtual Memory Translation

- Every virtual address **must** to be translated into a physical address before data is accessed.

- `int k = j + 3;`

- To look up the data stored in virtual address `&j...`

- Translate virtual address `&j` into a physical address

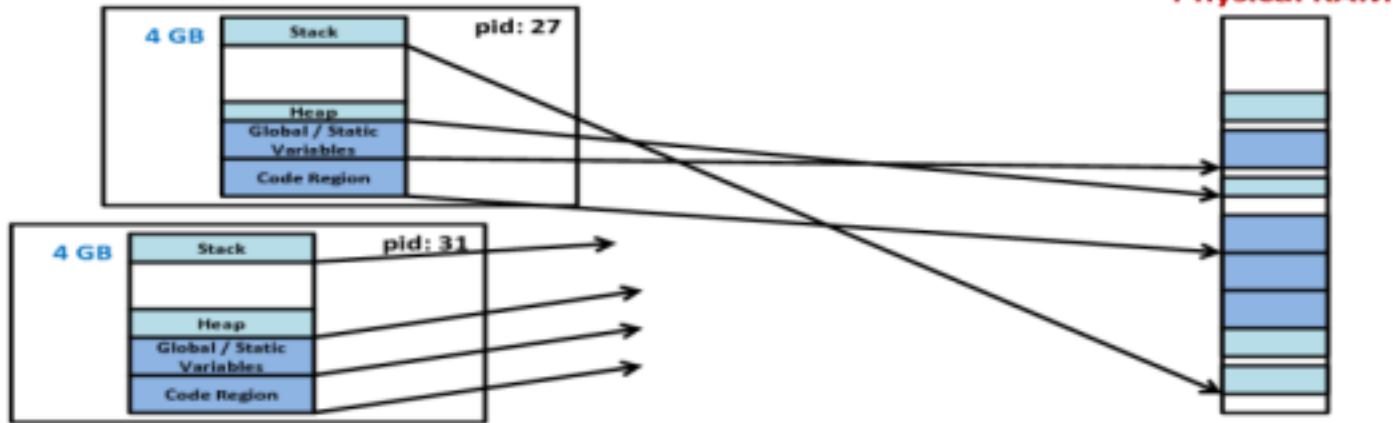
- Fetch that data from the location in RAM

- Return the data to the process

# Solution #1: Segmentation

- **Segmentation:** Place each logical piece of a program's memory into RAM at an offset.

## Virtual Memory



# Memory Segmentation

- **Advantages?**

- EASY

- FAST

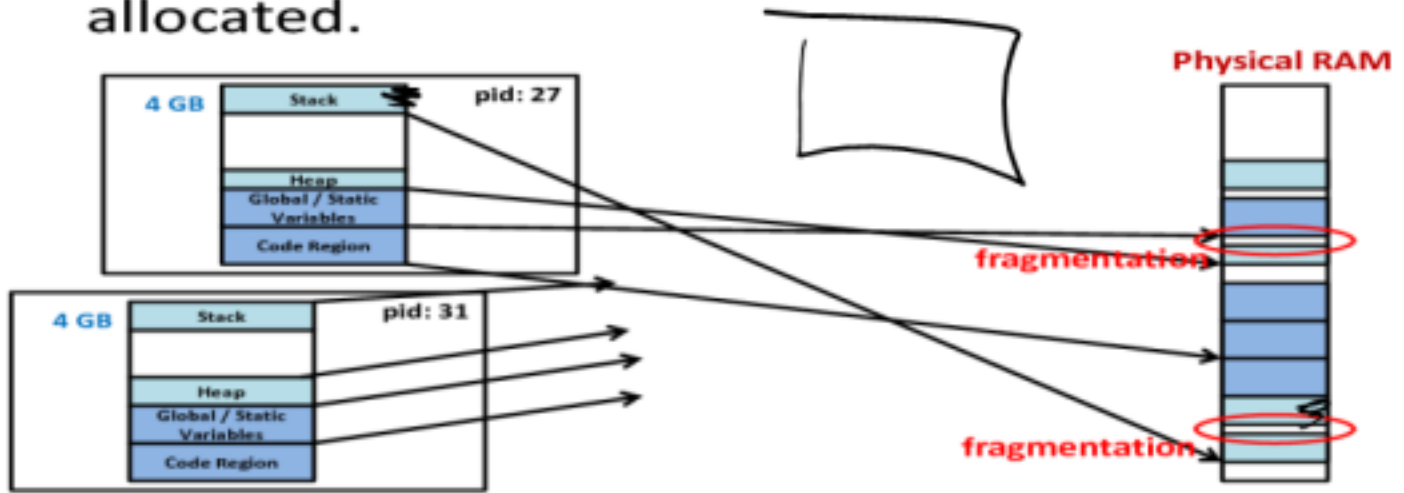
- **Disadvantages?**

- Limited RAM

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# Segmentation Disadvantage #1

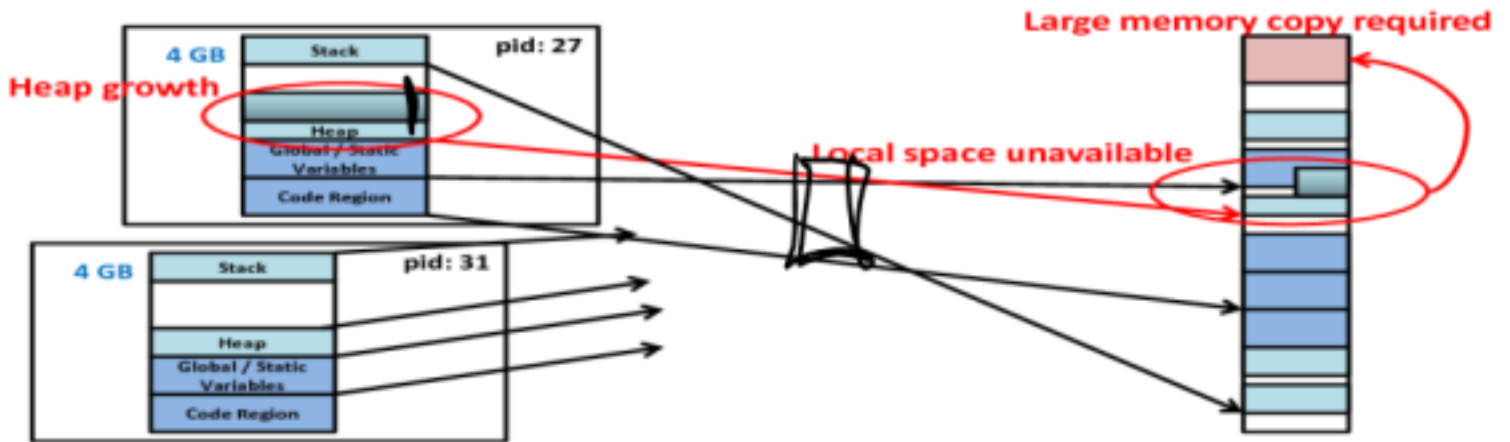
- **External Fragmentation:** Physical RAM will develop small holes over time, unable to be allocated.





# Segmentation Disadvantage #2

- **Storage Growth:** When memory usage grows, physical RAM must be allocated. If space is not available nearby, a large copy is required.



# Paging and Page Replacement

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# Paging

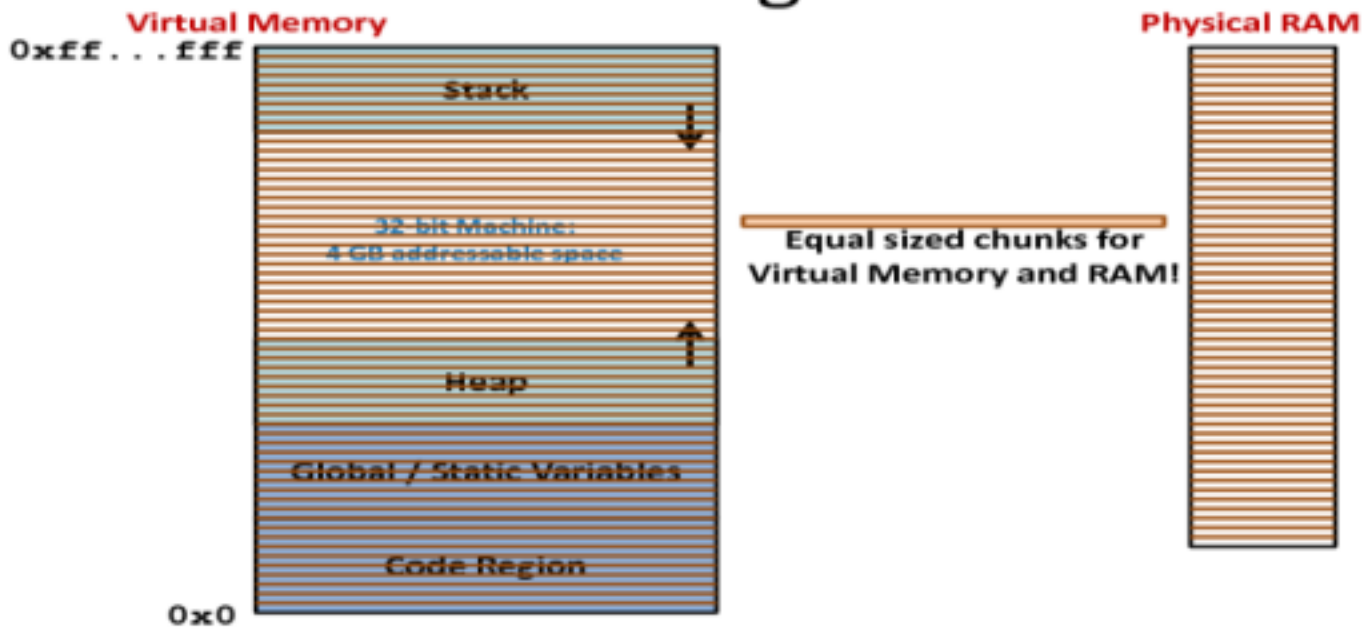
- Motivation:
    - Segmentation maps entire regions of memory to RAM, what happens if we scale this down?
  - Answer:
    - Paging
-

# Page

- Divide up **both** the **virtual address space** and the **physical RAM** into equal size chunks.
  - Each of these equal size chunks are called a **page**.
- Pages must always be of size  $2^N$ .
  - Eg: 1 KB, 2 KB, 4 KB, 8 KB, etc.

↳  $2^{12}$

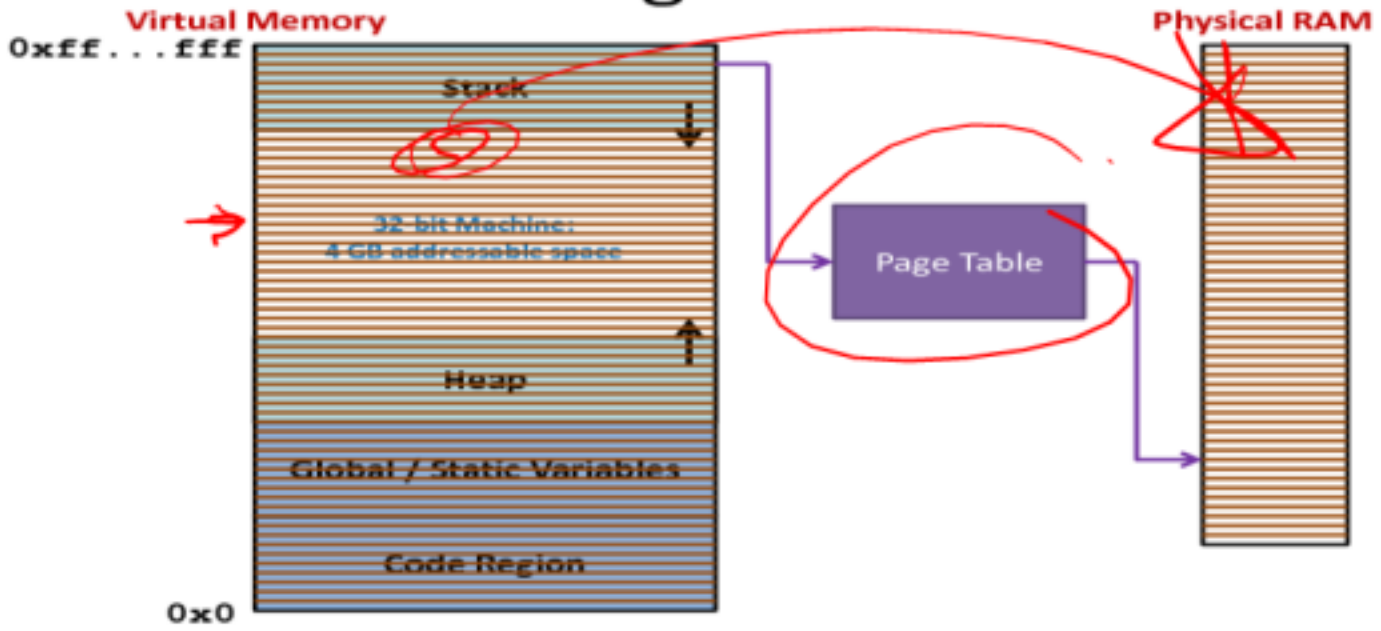
# Page



# Page Table

- A **page table** provides a mapping between each **virtual page** and the **physical page** in RAM.
-

# Page Table



# How does the Page Table work?

- Given a size of a page, you can always divide a virtual memory address into two pieces:
    - **Page Number / Page Table Index:** What virtual page are we on?
    - **Page Offset:** How far are we inside the page?
-



# How does the Page Table work?

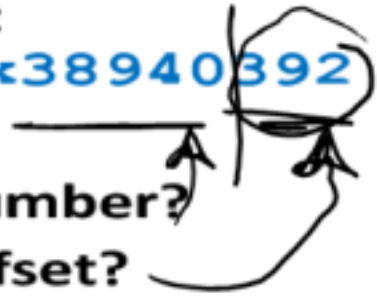
- Example
  - 4 KB pages

→ 2/2 BYTES → 12 BITS

- Virtual Address:

0x38940392

- Virtual Page Number?
- Virtual Page Offset?



# How does the Page Table work?

- Example

- 256 B pages

→  $2^8 = 8 \text{ BITS}$

- Virtual Address:

0x38940392

- Virtual Page Number?

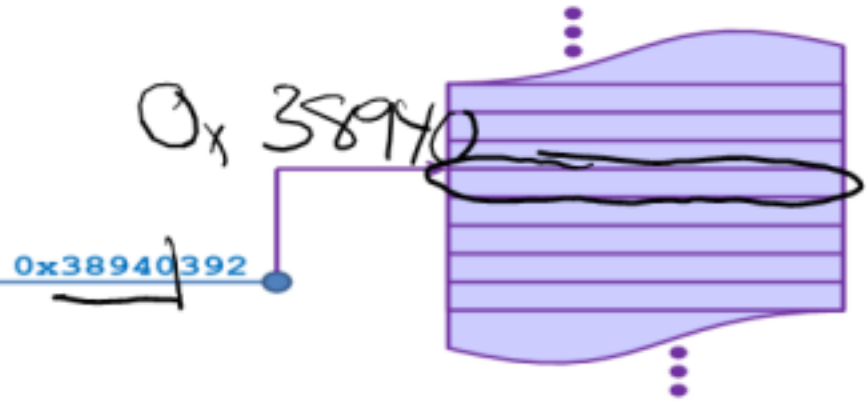
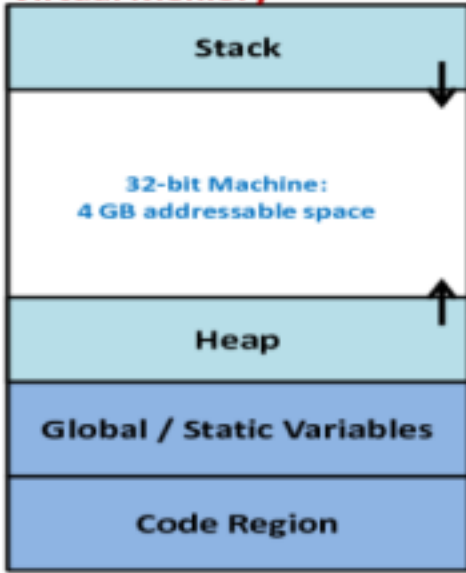
- Virtual Page Offset?



# Page Table

Assume 4 KB pages.

## Virtual Memory



# Page Table Entries

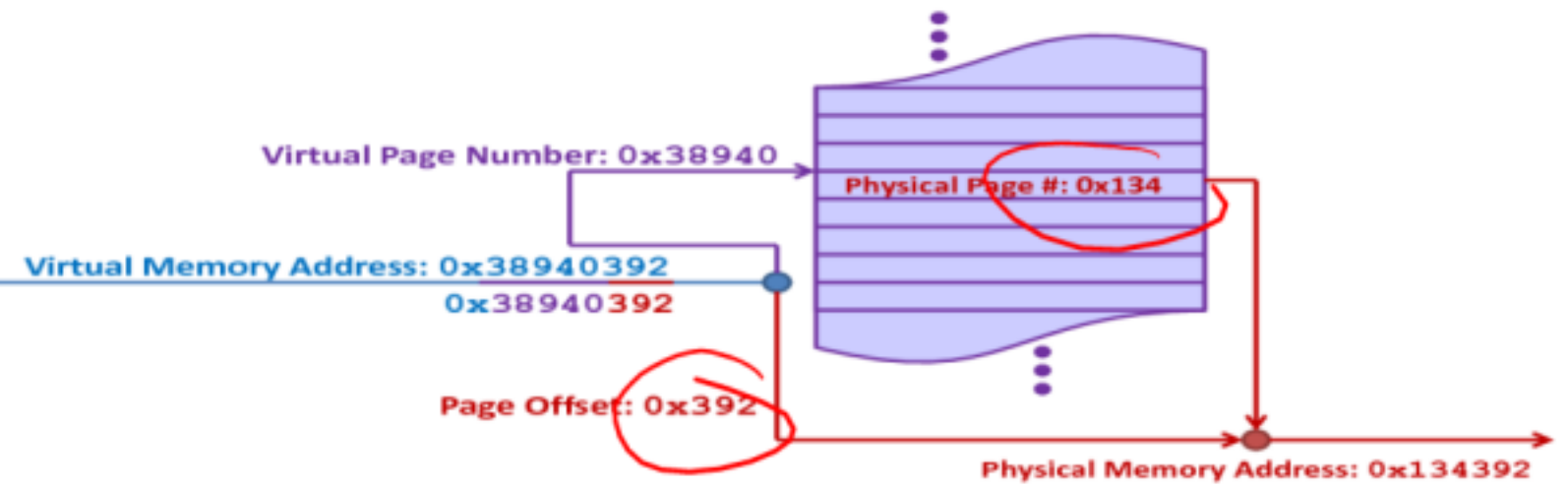
- What is the most important thing in each entry in the Page Table, or each **Page Table Entry (PTE)**?

WHERE ARE YOU??  
(IN RAM)

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# Page Table

Assume 4 KB pages.



# Modern Systems...

- A modern economy laptop may have 2 GBs of RAM...
    - ...may not be enough RAM for all those programs you run! :(
-

# Resident Bit

- **Solution:** Allow the page table to translate both to RAM and to a hard drive!
  - How?
    - **Resident Bit:** A single bit in every page table entry.
      - **1: Resident in RAM,** use the physical page number to translate the virtual address to a physical address.
      - **0:** Not resident in RAM, but it is **on disk.** Instead of a physical page number, a disk page number of the data.
-

# A Really Simple System...

- For an example, we have a system with some really simple properties:
  - 4 KB pages
  - Only 16 KB of RAM
    - Eg: Only 4 total pages.
- **Q:** How many bits are in a physical memory address?

$$2^{14} \rightarrow 14$$




# A Really Simple System...

Physical RAM

0x3000
0x2000
0x1000
0x0

# A Really Simple System...

- Virtual Page #: 17 ✓
- Virtual Page #: 33 ✓
- Virtual Page #: 40 ✓
- Virtual Page #: 17 ✓
- Virtual Page #: 43 ✓
- Virtual Page #: 8 ✓
- Virtual Page #: 99 ✓
- Virtual Page #: 33 ✓
- Virtual Page #: 99 ✓
- Virtual Page #: 17 ✓

LEAST  
RECENTLY  
USED

Physical RAM

→ <del>3</del> 17	0x3000
→ <del>2</del> 99	0x2000
→ <del>8</del> 8	0x1000
→ <del>3</del> 3	0x0

4

# A Really Simple System...

Virtual Page #: 17

Virtual Page #: 33

Virtual Page #: 40

Virtual Page #: 17

Virtual Page #: 43

Virtual Page #: 8

Virtual Page #: 99

Virtual Page #: 33

Virtual Page #: 99

Virtual Page #: 17

OPTIMAL

- VERY HARD  
TO PREDICT

Physical RAM

45 99  
0x3000

40 8  
0x2000

33  
0x1000

17  
0x0

2

# A Really Simple System...

Virtual Page #: 17 →

Virtual Page #: 33 →

Virtual Page #: 40 →

Virtual Page #: 17 →

Virtual Page #: 43 →

Virtual Page #: 8 →

Virtual Page #: 99 →

Virtual Page #: 33 →

Virtual Page #: 99 →

Virtual Page #: 17 →

LEAST  
FREQ.  
USED

TCE: LRU

Physical RAM

<del>40</del> 33 0x3000
<del>40</del> 99 0x2000
<del>33</del> 8 0x1000
17 0x0

3

# A Really Simple System...

- Virtual Page #: 17 → ✓
- Virtual Page #: 33 → ✓
- Virtual Page #: 40 → ✓
- Virtual Page #: 17 → ✓
- Virtual Page #: 43 → ✓
- Virtual Page #: 8 → ✓
- Virtual Page #: 99 → ✓
- Virtual Page #: 33 → ✓
- Virtual Page #: 99 → ✓
- Virtual Page #: 17 → ✓

Most  
RECENTLY  
USED

## Physical RAM

43899	0x3000
40	0x2000
33	0x1000
17	0x0



# A Really Simple System...

- Virtual Page #: 17 → ✓
- Virtual Page #: 33 → ✓
- Virtual Page #: 40 → ✓
- Virtual Page #: 17 → ✓
- Virtual Page #: 43 → ✓
- Virtual Page #: 8 → ✓
- Virtual Page #: 99 → ✓
- Virtual Page #: 33 → ✓
- Virtual Page #: 99 → ✓
- Virtual Page #: 17 → ✓

FIFO

Physical RAM

4317	0x3000
4033	0x2000
3399	0x1000
178	0x0

→

→

④

# A Really Simple System...

Virtual Page #: 17 →

Virtual Page #: 33 →

Virtual Page #: 40 →

Virtual Page #: 17 →

Virtual Page #: 43 →

Virtual Page #: 8 →

Virtual Page #: 99 →

Virtual Page #: 33 →

Virtual Page #: 99 →

Virtual Page #: 17 →

**Physical RAM**

0x3000
0x2000
0x1000
0x0

# A Really Simple System...

Virtual Page #: 17 →

Virtual Page #: 33 →

Virtual Page #: 40 →

Virtual Page #: 17 →

Virtual Page #: 43 →

Virtual Page #: 8 →

Virtual Page #: 99 →

Virtual Page #: 33 →

Virtual Page #: 99 →

Virtual Page #: 17 →

**Physical RAM**

0x3000
0x2000
0x1000
0x0



# A Really Simple System...

Virtual Page #: 17 →

Virtual Page #: 33 →

Virtual Page #: 40 →

Virtual Page #: 17 →

Virtual Page #: 43 →

Virtual Page #: 8 →

Virtual Page #: 99 →

Virtual Page #: 33 →

Virtual Page #: 99 →

Virtual Page #: 17 →

**Physical RAM**

0x3000
0x2000
0x1000
0x0

# A Really Simple System...

Virtual Page #: 17 →

Virtual Page #: 33 →

Virtual Page #: 40 →

Virtual Page #: 17 →

Virtual Page #: 43 →

Virtual Page #: 8 →

Virtual Page #: 99 →

Virtual Page #: 33 →

Virtual Page #: 99 →

Virtual Page #: 17 →

**Physical RAM**

0x3000
0x2000
0x1000
0x0

# Five Page Replacement Algorithms

- Optimal

- FIFO

- LRU

- LFU

- MRU

← WIDELY USED

← NOT SO MUCH

# Five Page Replacement Algorithms

- **Optimal**
  - **FIFO**
  - **LRU**
  - **LFU**
  - **MRU**
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